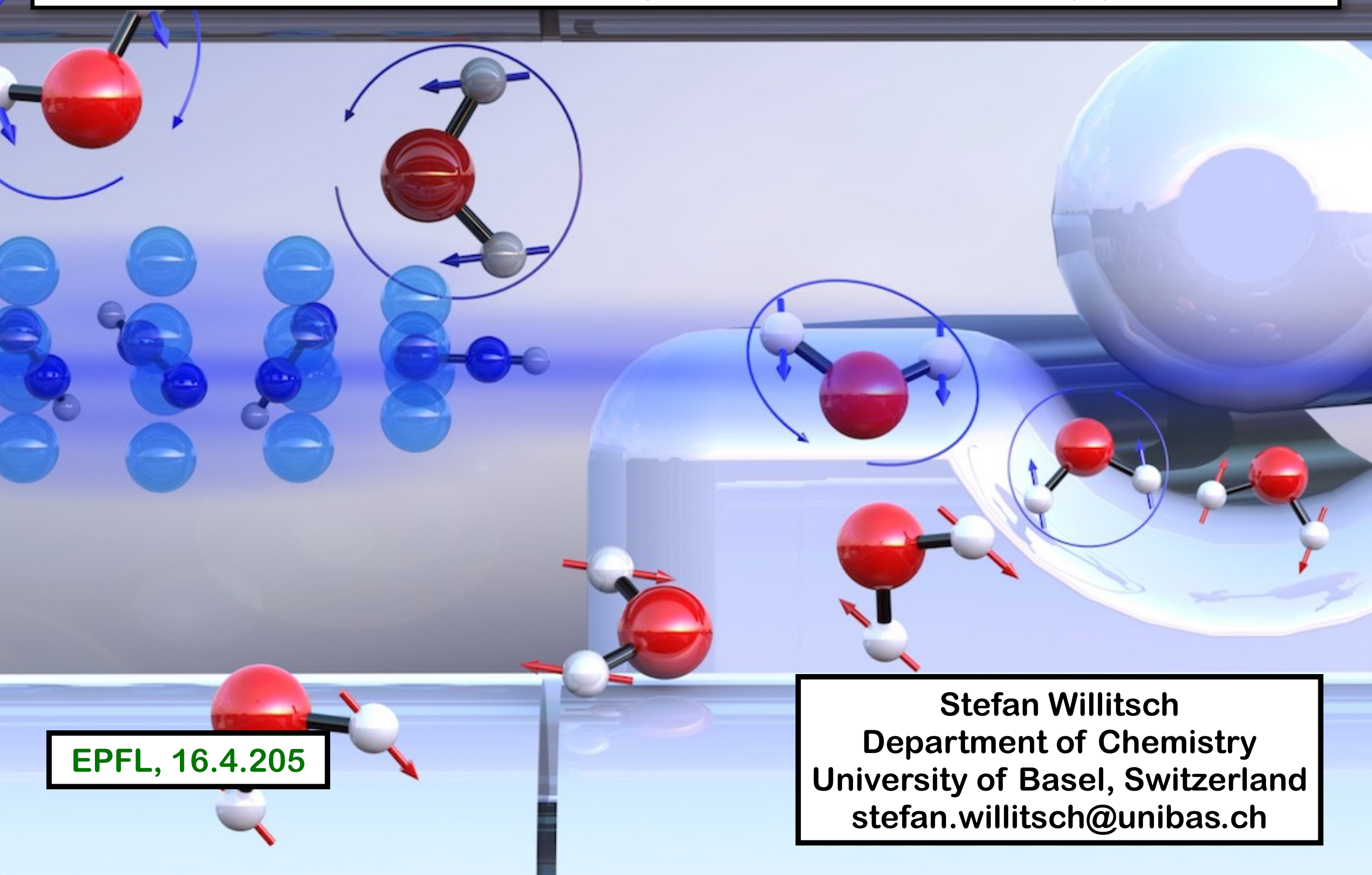


Cold molecular ions in traps: methods and applications



EPFL, 16.4.205

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University of Basel, Switzerland
stefan.willitsch@unibas.ch

Applications of cold molecular ions in physics and chemistry

Quantum control over single trapped particles

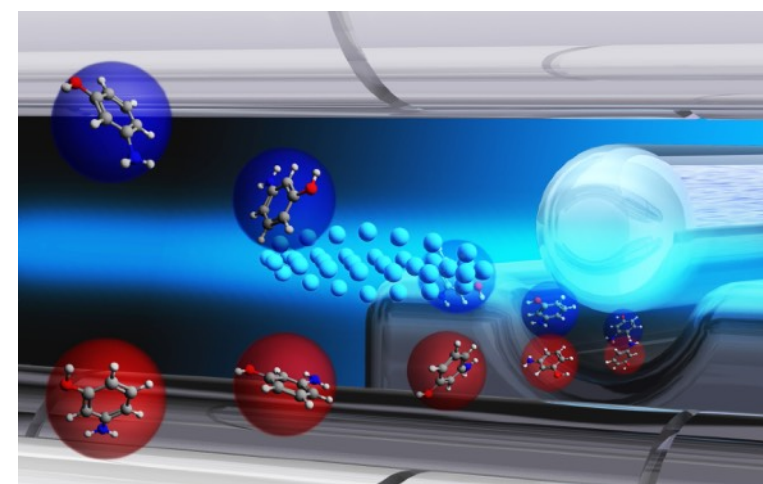
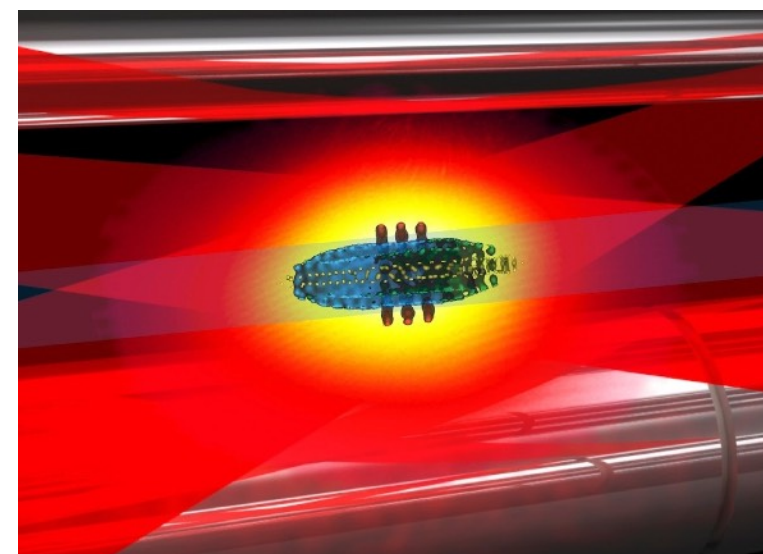
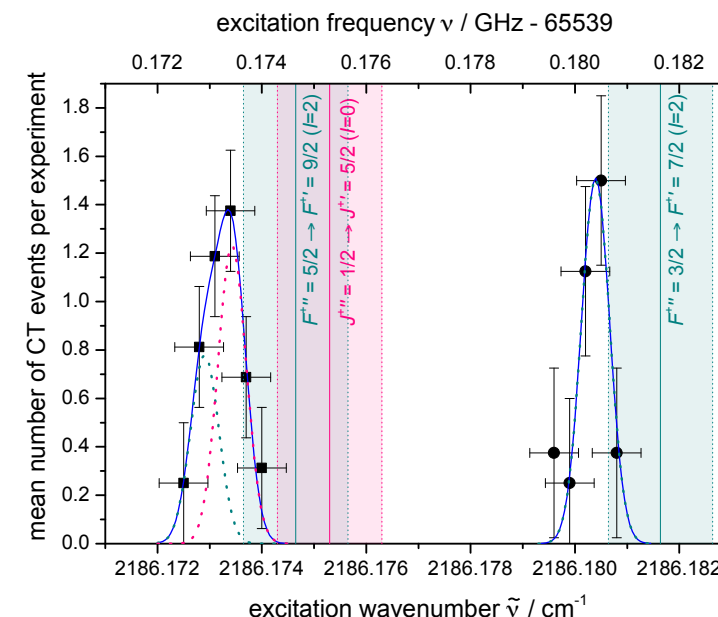
- Quantum logic and quantum technologies
- Precision spectroscopy

Ion-neutral interactions, collisions and chemical reactions in a new physical regime

- Study “exotic” chemical processes
- Explore quantum character of collisions
- Probe fine details of intermolecular interactions

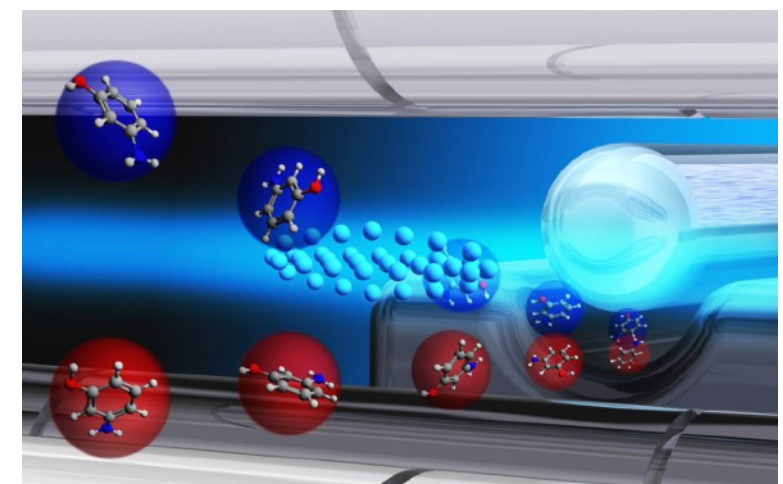
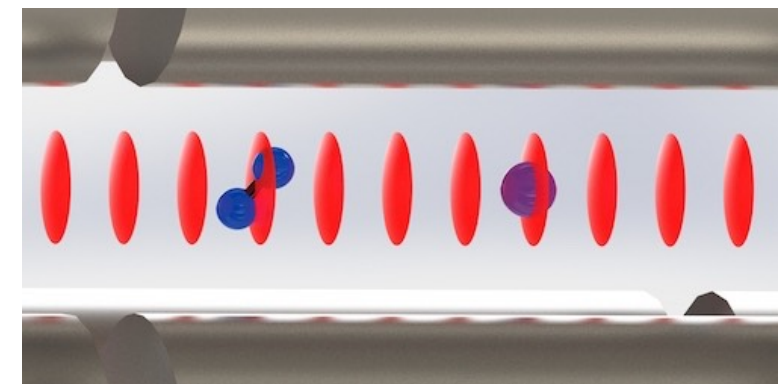
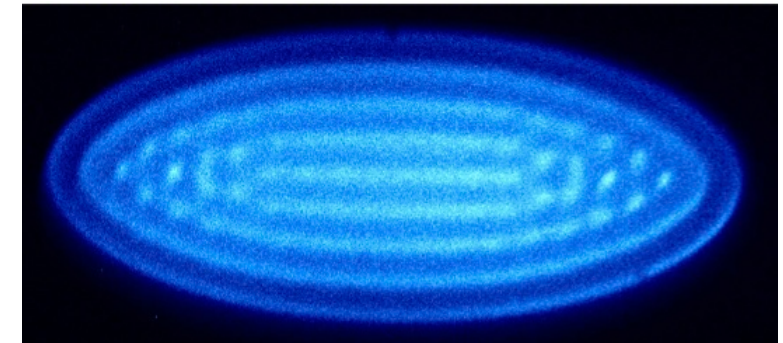
New methods for studying and controlling chemical reactions

- Accurate quantum-state AND collision-energy control
- Controlled chemistry of large molecules



Contents

1. Cooling and trapping of molecular ions:
basic techniques
2. Internal-state preparation of cold molecular ions
3. Applications:
 1. Molecular-ion quantum technologies and quantum-logic spectroscopy
 2. Unravelling the details of chemical reaction mechanisms with controlled molecules



Recommended books on cold ions

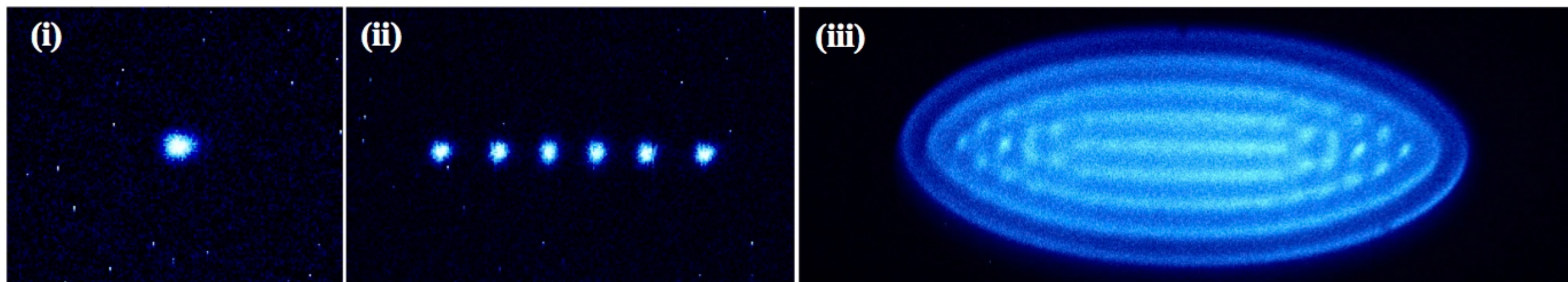
- A. Osterwalder, O. Dulieu (ed.), Cold Chemistry, RSC Publishing, 2018
- F. G. Major et al., Charged Particle Traps Vol. I+II, Springer, 2005 + 2007
- M. Knoop et al. (ed.), Ion Traps For Tomorrow's Applications, Proc. Int. School Phys. E. Fermi Vol. 189, IOS Press, 2015
- M. Knoop et al. (ed.), Trapped Charged Particles, World Scientific, 2016 R.V.
Krems et al. (ed.), Cold Molecules, CRC Press 2009

Recommended review articles

- M. Sinhal and S. Willitsch, "Molecular-ion quantum technologies" in "Photonic Quantum Technologies: Science and applications", ed. M. Benyoucef, Wiley-VCH 2023 (arXiv:2204.08814)
- M. Deiß, S. Willitsch and J. H. Denschlag, "Cold trapped molecular ions and hybrid platforms for ions and neutral particles", Nat. Phys. 20 (2024), 713 (arXiv:2311.12640)
- S. Willitsch, "Chemistry with Controlled Ions", Adv. Chem. Phys. 162 (2017), 307

1. Cooling and trapping of molecular ions: basic techniques

Cold ions in traps: ion Coulomb crystals



Fluorescence images of laser-cooled Ca^+ ions in an ion trap

Properties of Coulomb-crystallized ions:

- Cold (μK -mK)
- Long trapping times ($> \text{hrs}$)
- Ordered structures of single, localized particles:
observe, address and manipulate single ions on the quantum level

Lit.: • D. Leibfried et al., Rev. Mod. Phys. 75 (2003), 281
 • H. Häffner et al., Phys. Rep. 469 (2008), 155
 • S. Willitsch, Int. Rev. Phys. Chem. 30 (2012), 175

RF ion trapping

- Trapping = confine particles in a suitable potential minimum. For the trapping of ions electric potentials Φ are an obvious choice.

- The Laplace equation $\left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} \right) \Phi = 0$

forbids the formation of a potential minimum with **static** electric fields in 3D space.

- Solution: **radiofrequency ion traps**

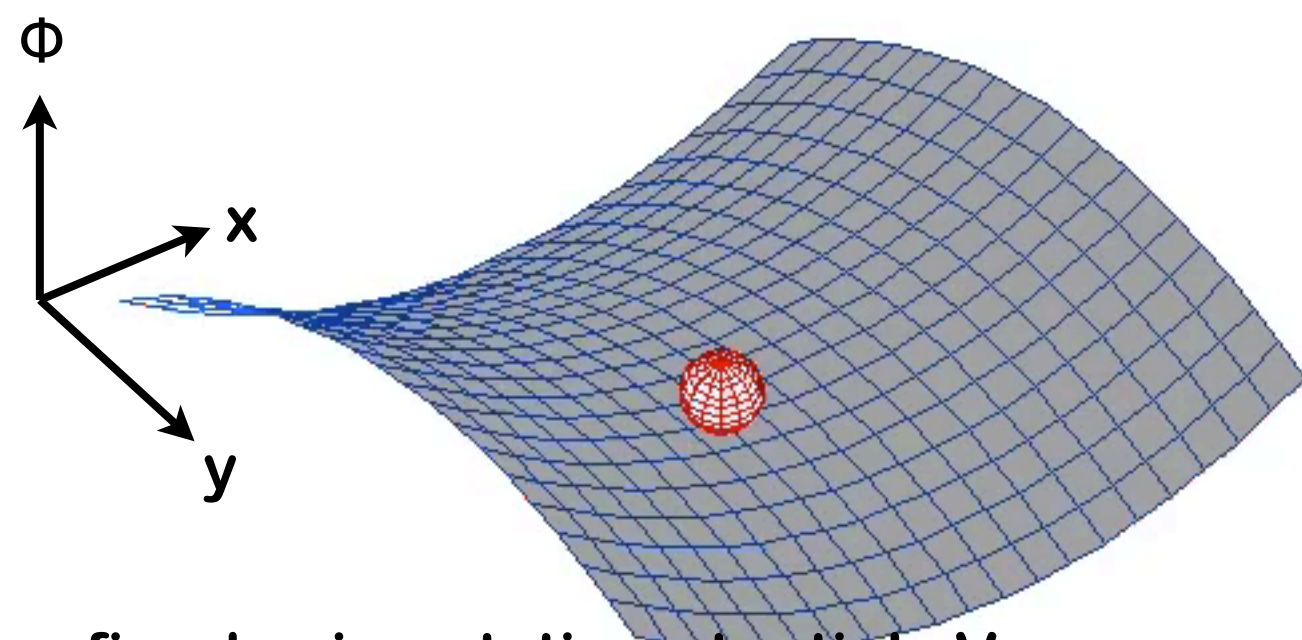
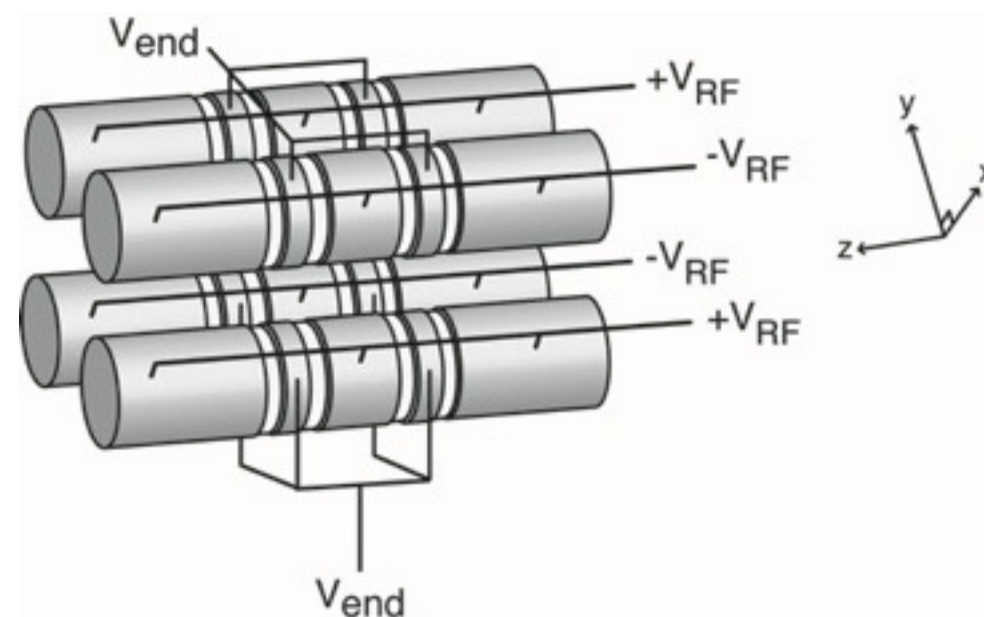
Trap ions dynamically in the x, y plane using time-varying voltages V_{RF} applied to the electrodes:

$$V_{RF} = V_{RF,0} \cos(\Omega_{RF} t)$$

- Linear Paul trap:** four electrodes arranged in a quadrupolar configuration

- The RF fields create a rotating potential saddle point which dynamically confines the ions.

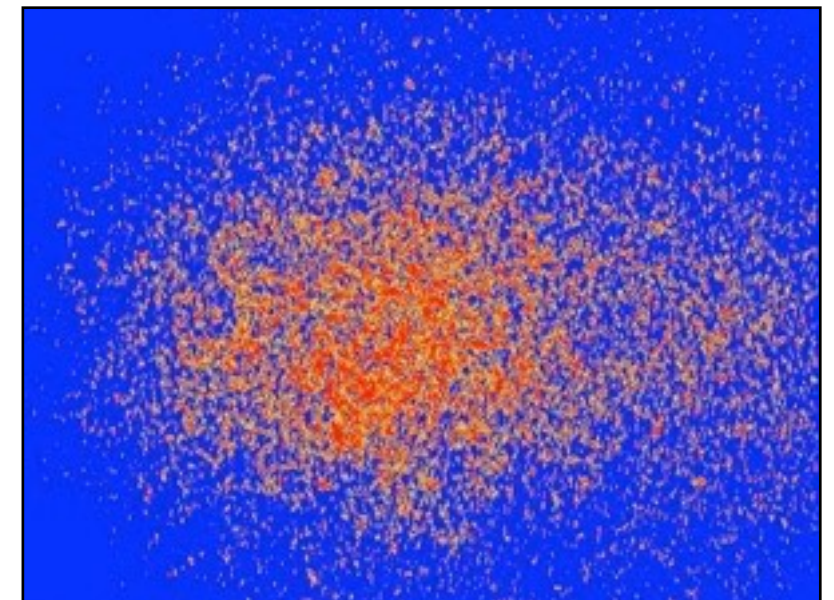
- Along the trap axis (= z axis) the ions are confined using static potentials V_{end} applied to the “endcap electrodes”.



Coulomb crystals

- Ion Coulomb crystals = ordered structures of strongly localised cations in ion traps at very low temperatures $T \ll 1$ K.
- Termed in analogy to “Wigner crystals” (ordered structures of electrons in solids) originally predicted by E. Wigner (1934).
- The term “crystal” is actually a misnomer (no translational symmetry !)

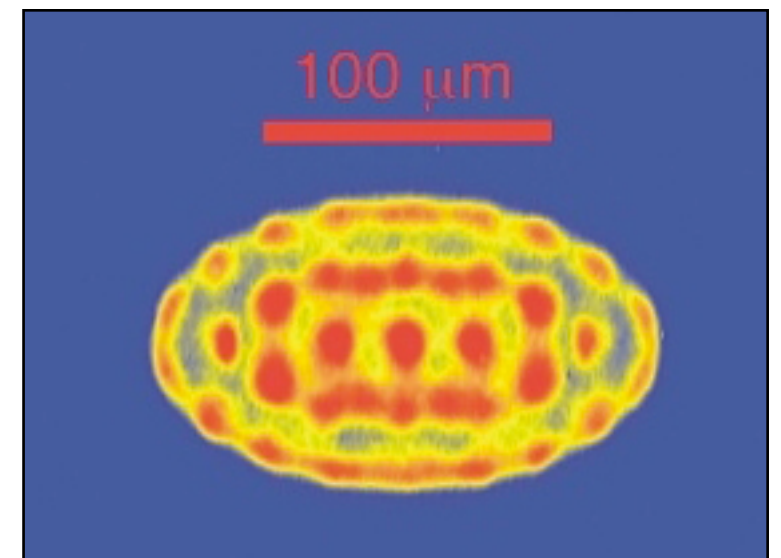
Warm Ca^+ ion cloud
in ion trap



Laser cooling

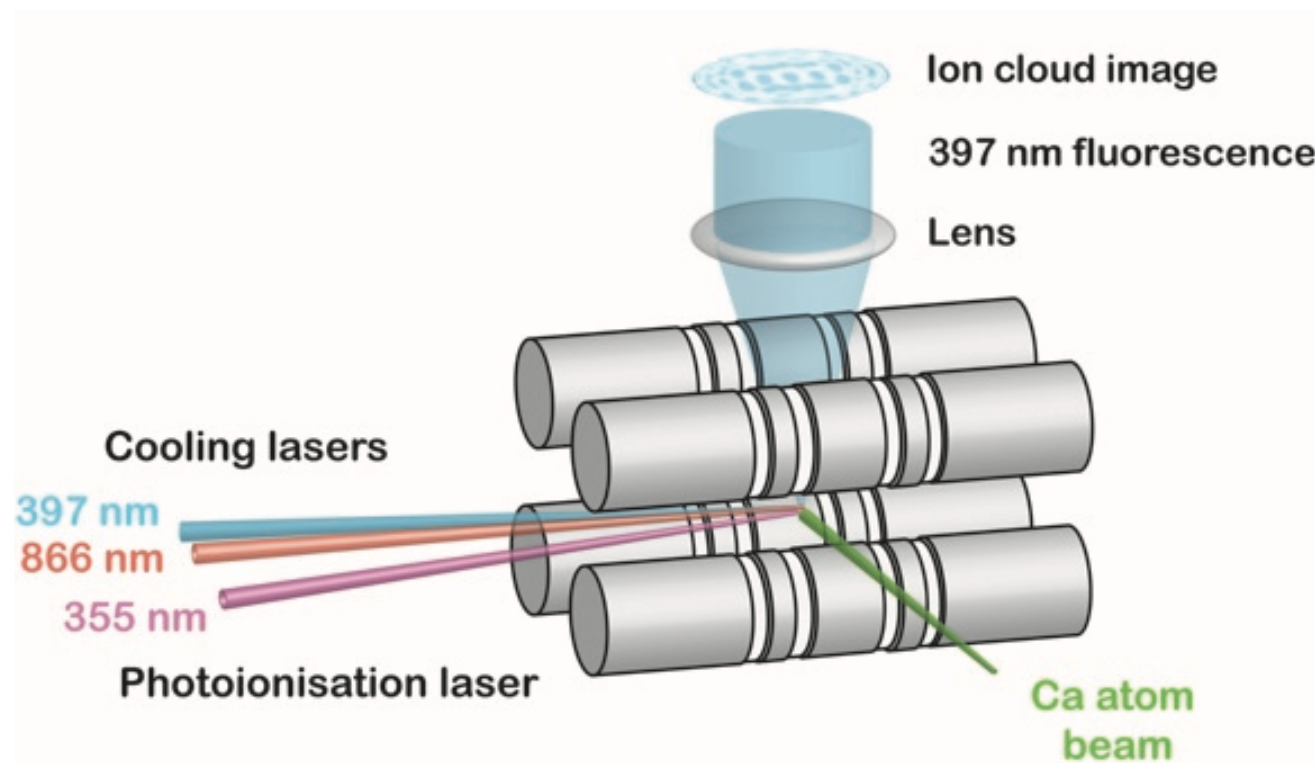


“Coulomb crystal”
at translational
temperatures
 $T \approx 10$ mK

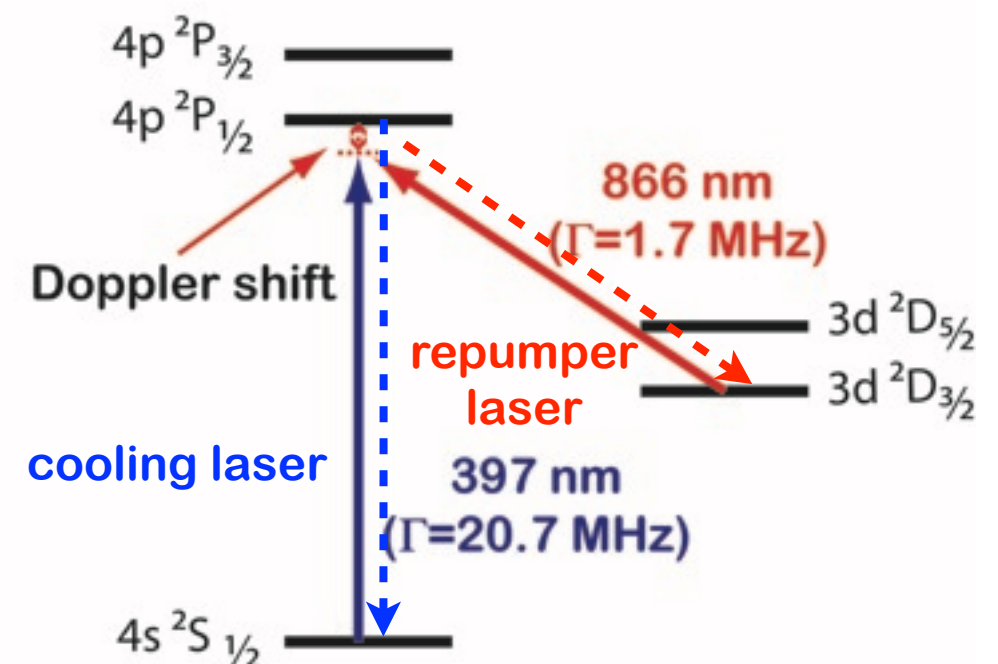


Laser cooling of trapped ions

- Typical ions used for laser cooling in traps are alkaline earth ions (Be^+ , Mg^+ , Ca^+ , Ba^+) often produced directly inside the trap by photoionisation of their neutral atoms.



Example: laser cooling of $^{40}\text{Ca}^+$

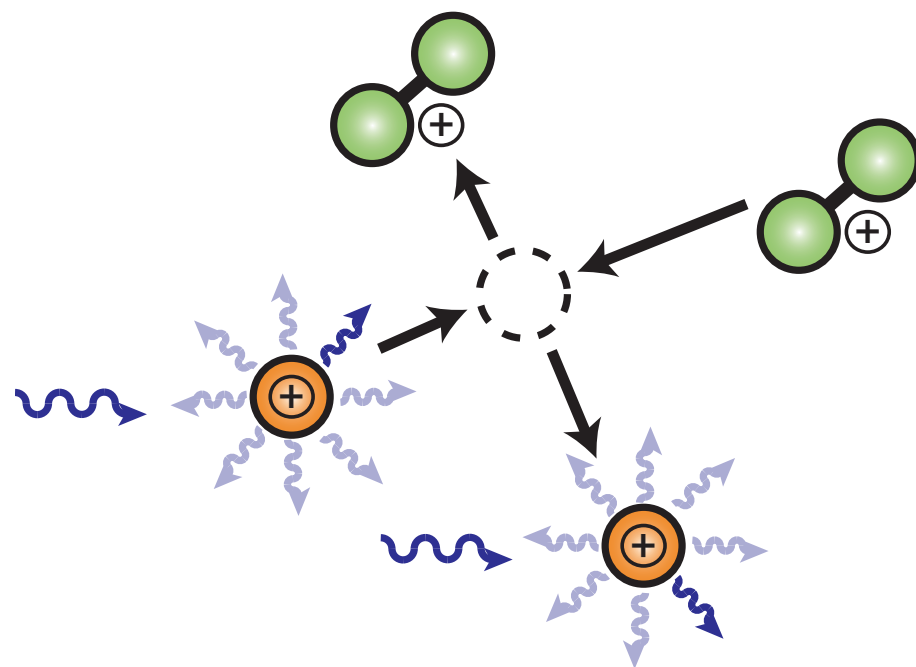


full lines = laser beams
dashed lines = spontaneous emission

Sympathetic cooling of molecular ions

Principle:

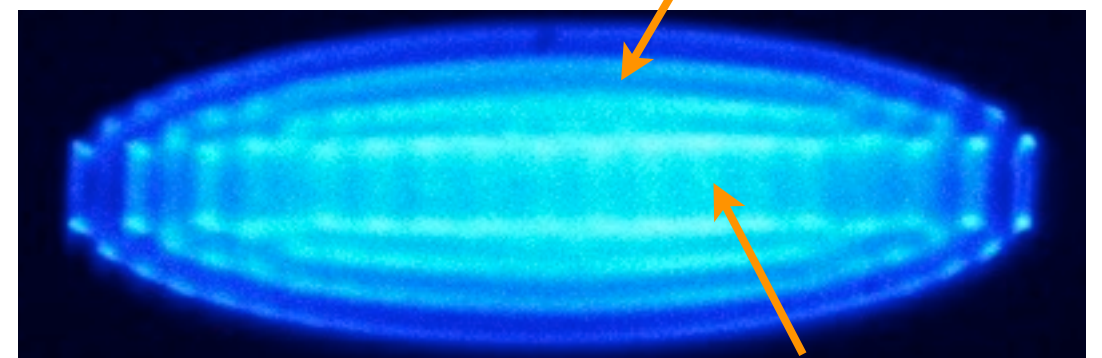
- Molecular ions are simultaneously trapped with laser-cooled atomic ions
- The molecular ions exchange kinetic energy in Coulomb-collisions with the atomic ions
- The energy is removed by laser cooling on the atomic ions



Molecular (or bi-component) Coulomb crystals:

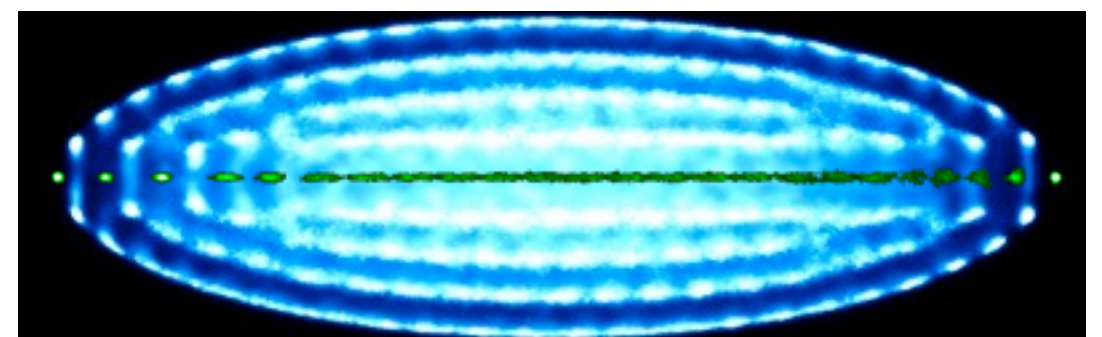
Experiment:

Laser-cooled Ca^+ ions



Sympathetically-cooled N_2^+ ions

Simulation:



2. Internal state preparation of cold molecular ions

Rotational laser cooling

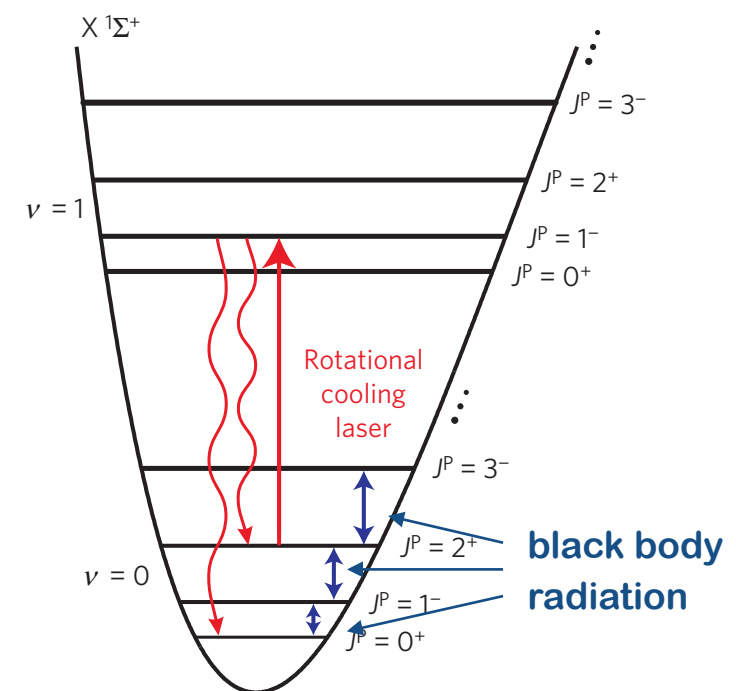
Staanum et al., Nature Phys. 6 (2010), 271
see also: Schneider et al., Nature Phys. 6 (2010), 275

Principle: sympathetically cool the translational motion of molecular ions and then use optical pumping by laser fields to accumulate the population in a specific rotational-vibrational level

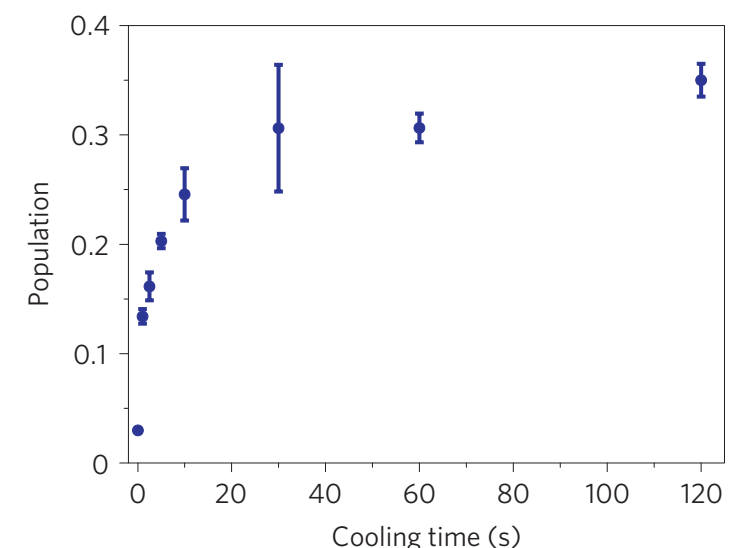
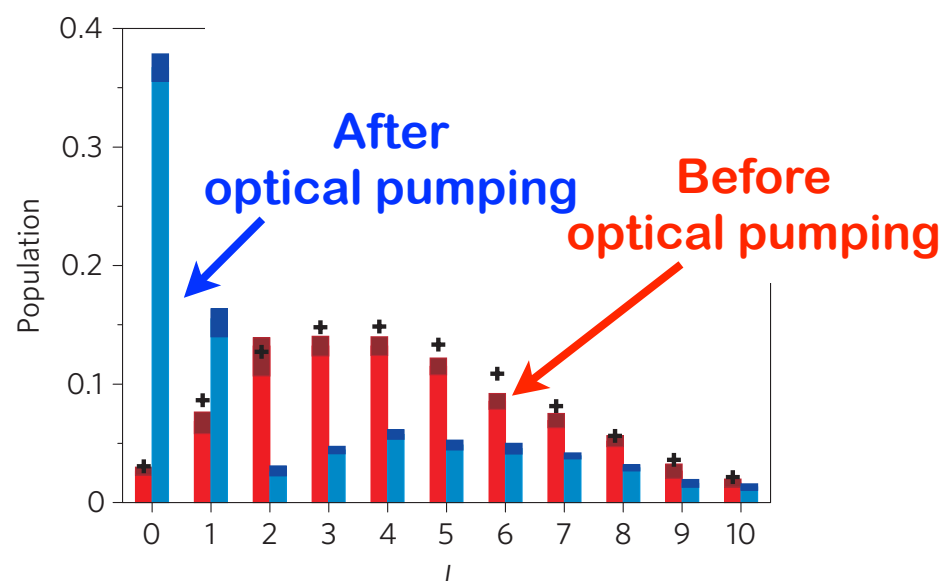
Example: MgH^+ . Use an IR laser to pump on the $v=0, J=2 \rightarrow v=1, J=1$ transition. The $v=1, J=1$ level can only fluoresce down to the $v=0, J=0$ and $J=2$ levels (selection rules!).

Transitions between rotational levels in the $v=0$ state induced by blackbody radiation constantly redistribute the population.

In combination with the optical pumping, an accumulation of the population in the $v=0, J=0$ level results.

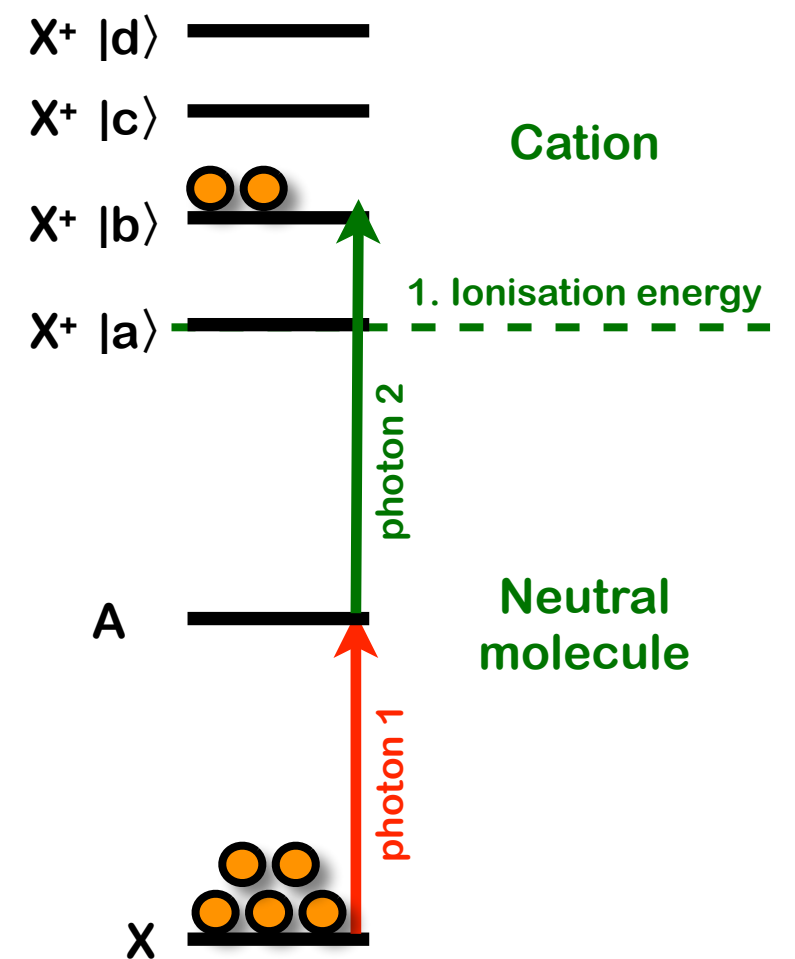


Ro-vibrational energy level scheme of MgH^+



Sympathetic cooling of state-prepared molecular ions

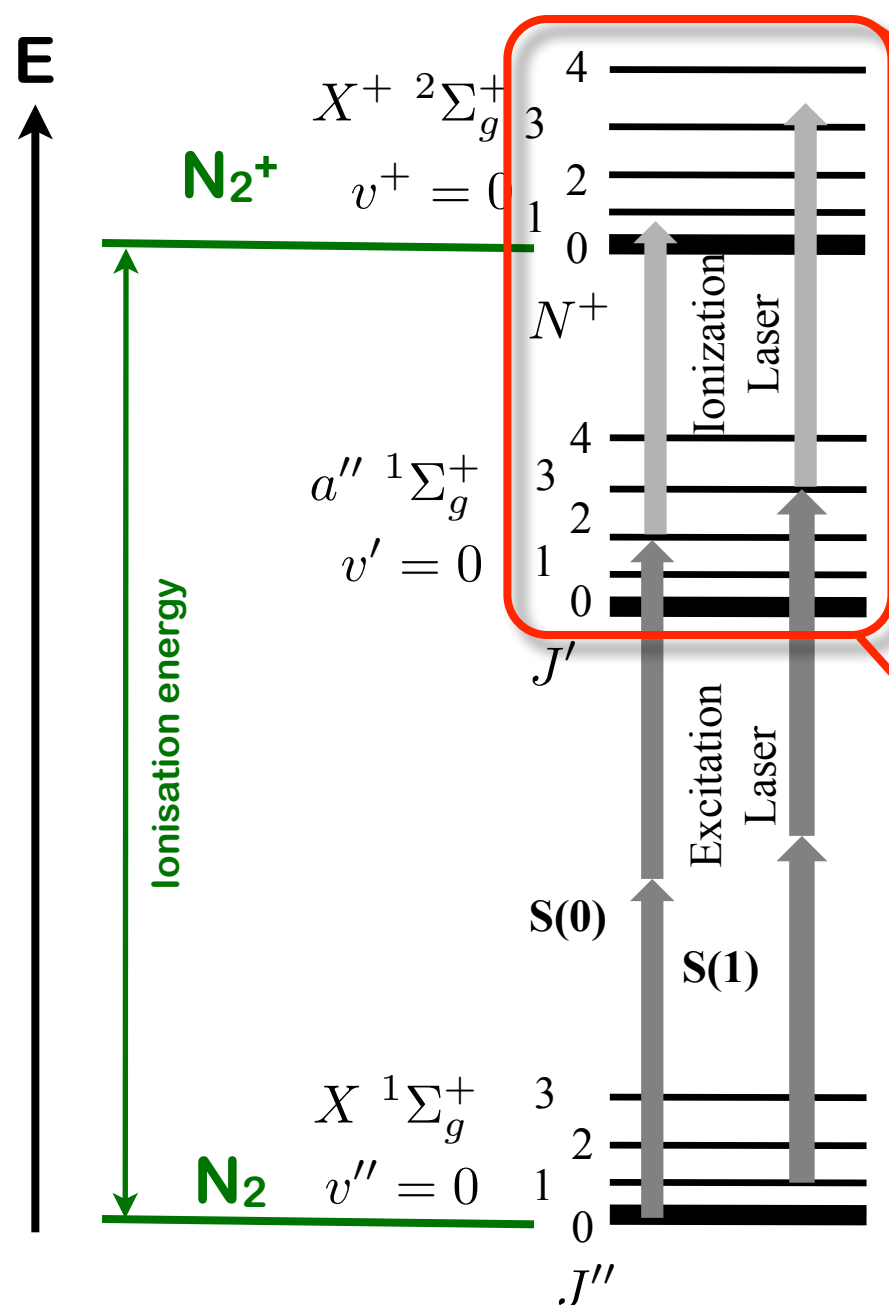
Principle: Prepare the molecular ions right from the beginning in a specific rotational-vibrational state by threshold photoionization of their neutral precursor molecules (i.e., photoionization just above a given ionization energy) and then sympathetically cool their translational motion.



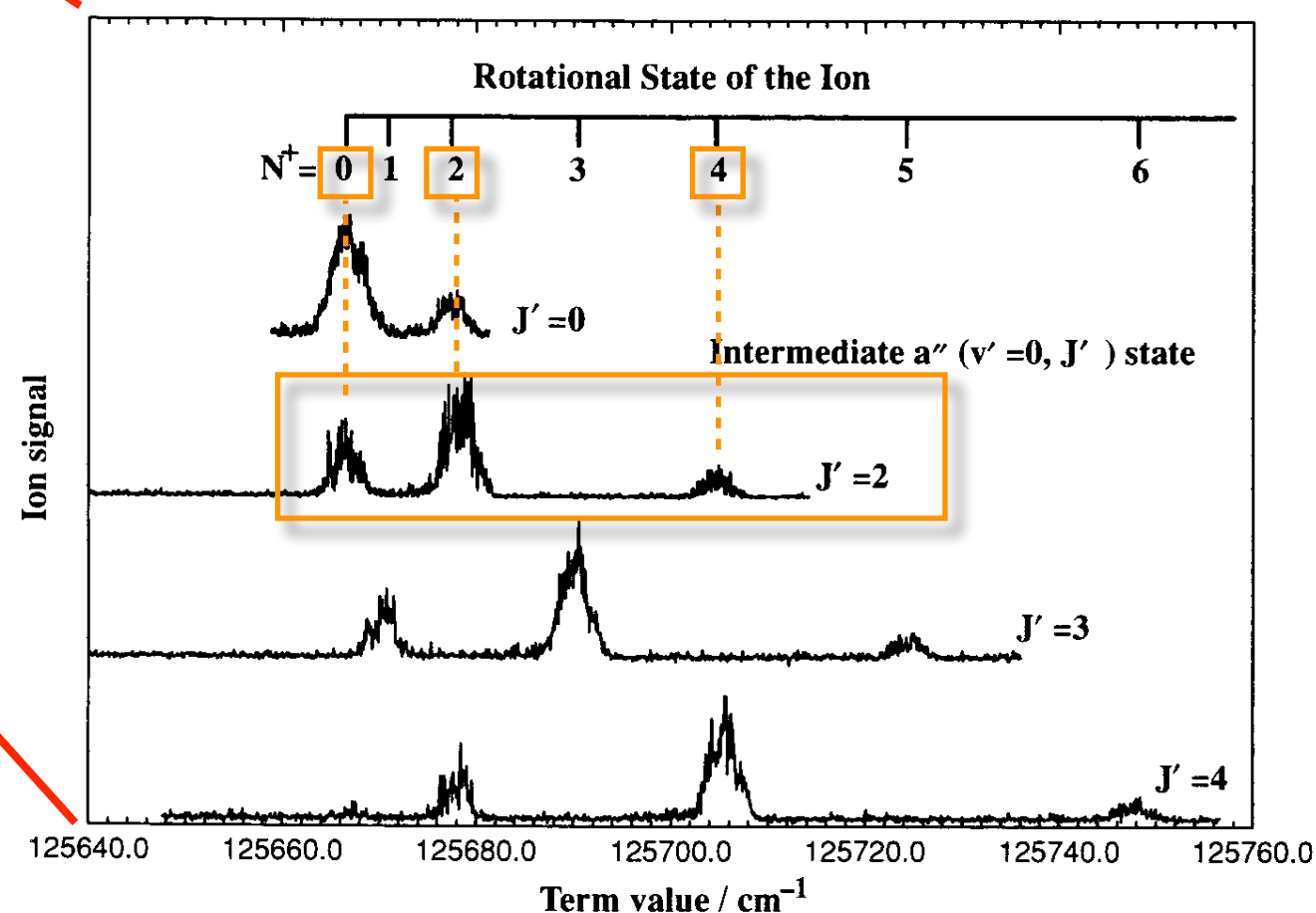
Threshold photoionization
of molecules

Example: threshold photoionization of N_2 :

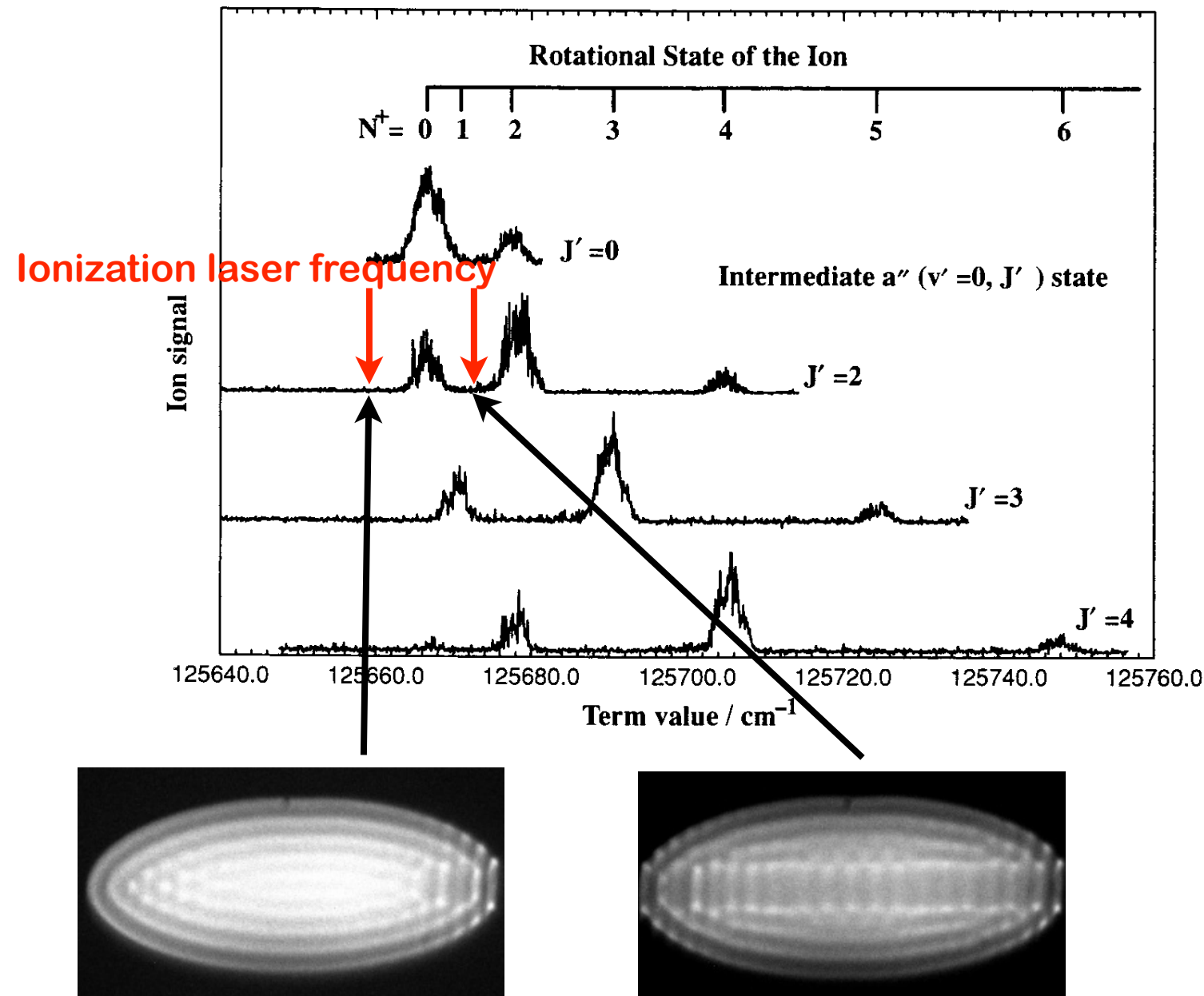
- [2+1']-photon resonance-enhanced threshold-photoionisation scheme for N_2



- Rotationally resolved photoelectron spectrum of N_2 showing the cationic rotational levels N^+ produced by threshold photoionisation out of well-defined intermediate rotational levels J'



- [2+1'] resonance-enhanced threshold photoionisation via the $a''\ ^1\Sigma_g^+$, $J'=2$ intermediate state of N_2 :



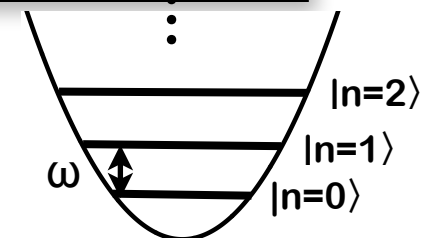
3. Applications: 1. Molecular-ion quantum technologies and quantum-logic spectroscopy

Resolved sideband cooling of ions into the quantum regime



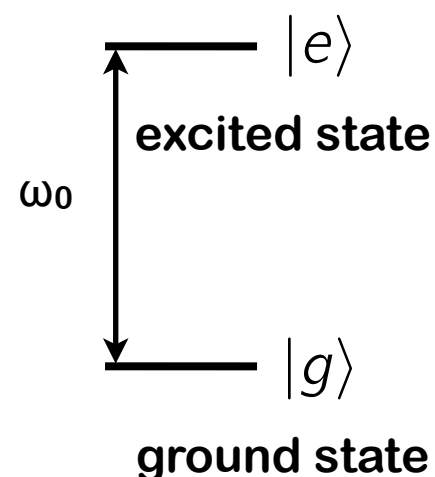
The motion of an ion in the harmonic pseudopotential of the ion trap corresponds to a **QM harmonic oscillator** problem:

- Motional states = the harmonic oscillator eigenstates $|n\rangle$, $n = 0, 1, 2, \dots$
- Motional states form a ladder of equidistant energy levels $E_n = \left(n + \frac{1}{2}\right) \hbar \omega$

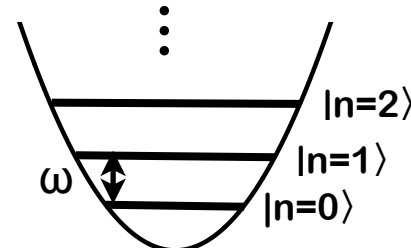


Resolved sideband cooling: cooling to the motional ground state by addressing the individual motional states

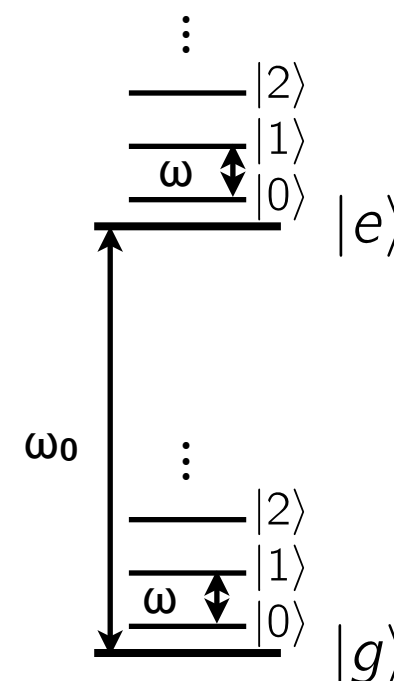
atomic two-level system



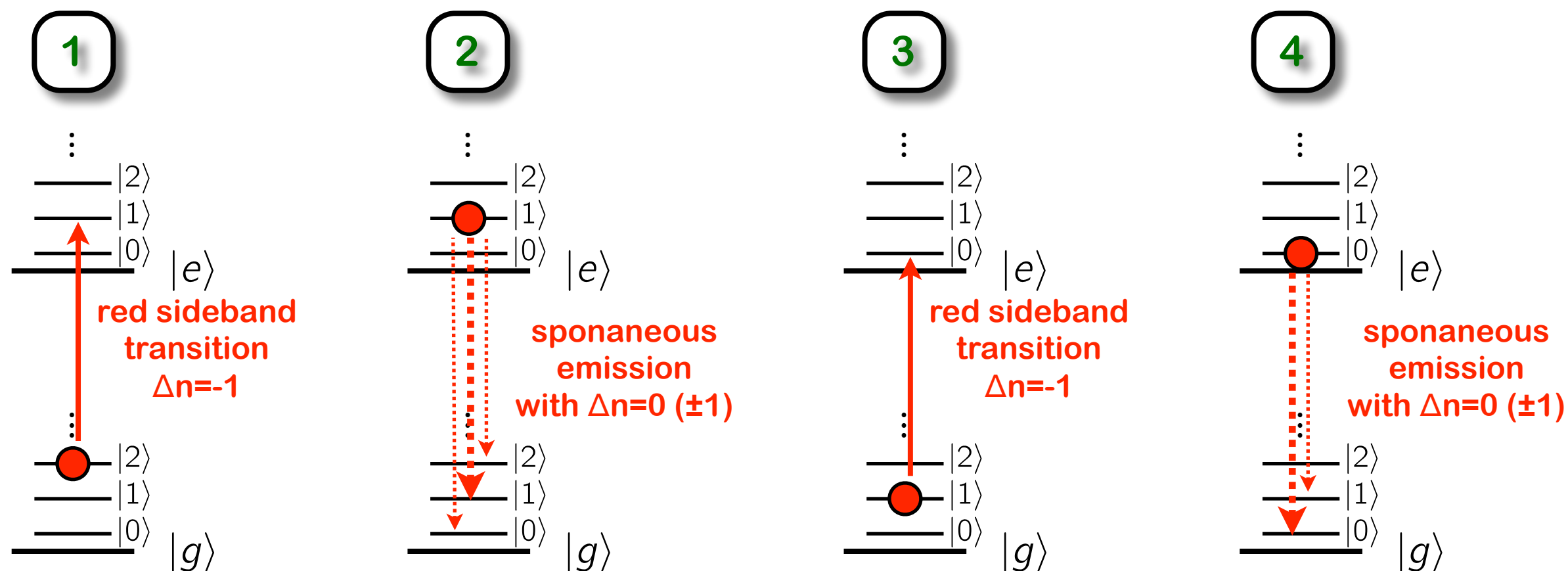
motional states in ion trap



=



Simple resolved sideband cooling scheme:

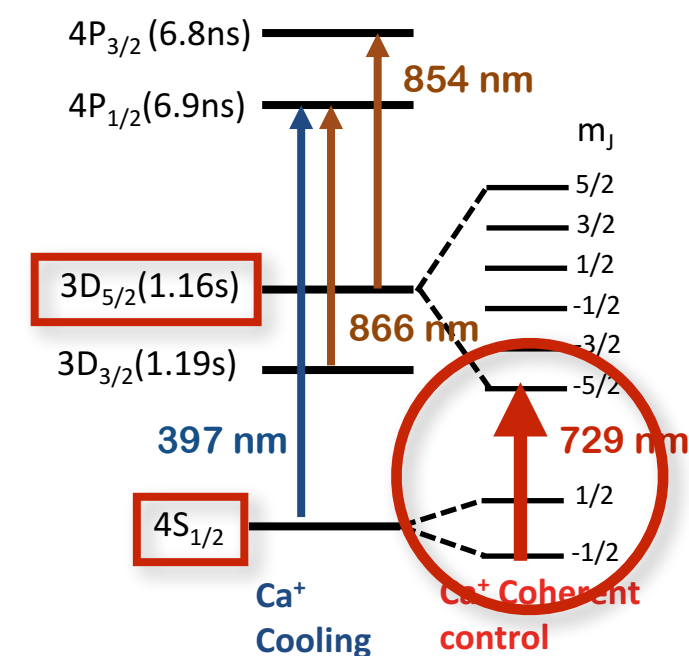
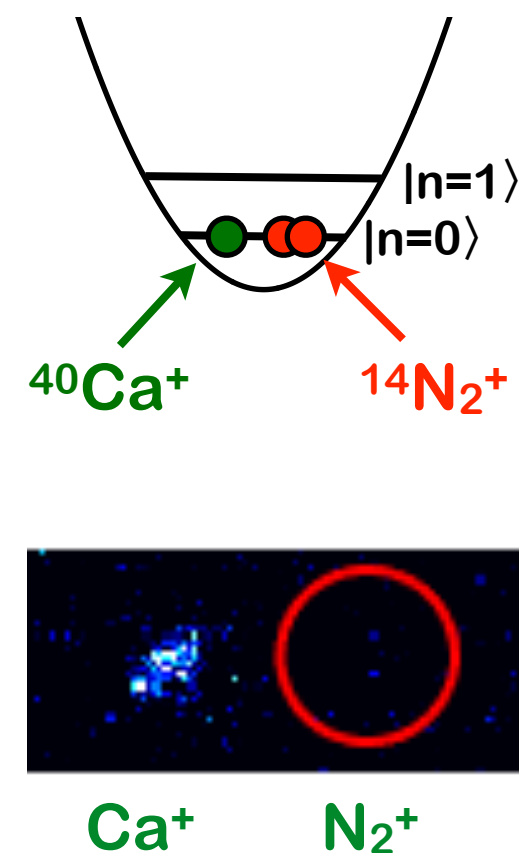
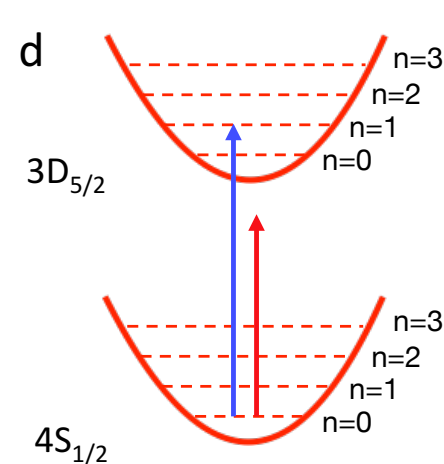
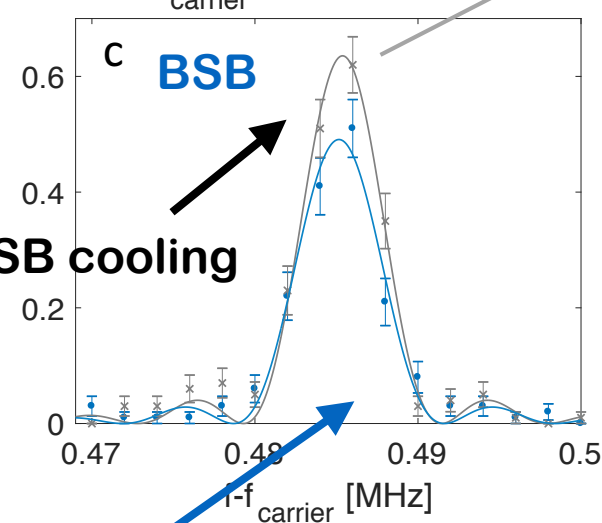
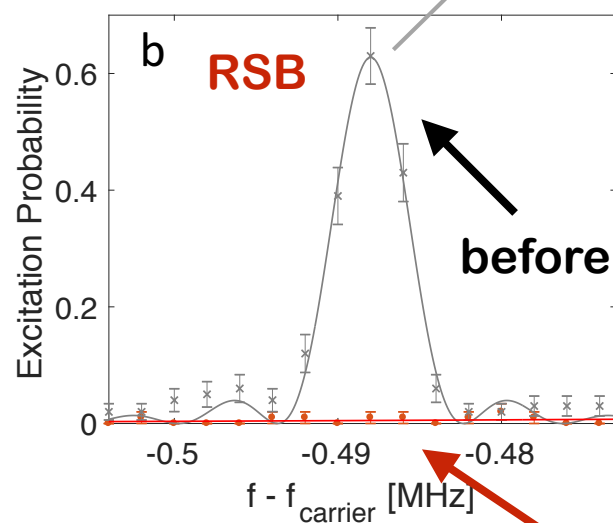
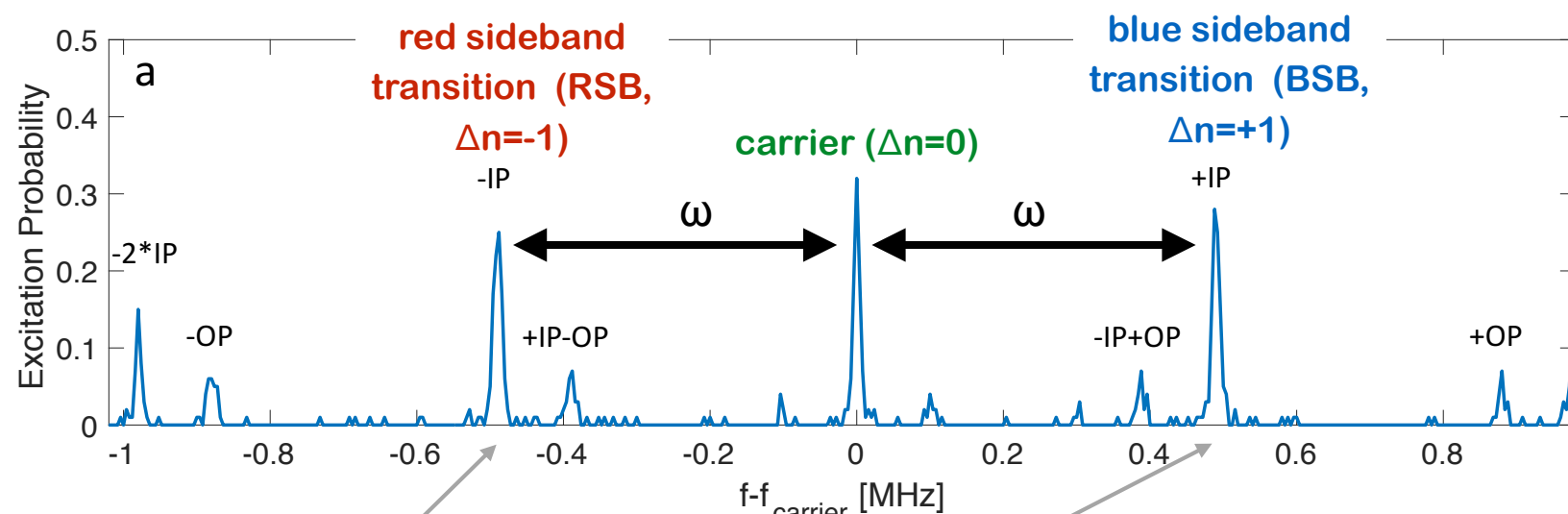


Lit.: D. Leibfried et al., Rev. Mod. Phys. 75 (2003), 281

H. Häffner et al., Phys. Rep. 469 (2008), 155



Example: Resolved-sideband cooling and spectroscopy of the $\text{Ca}^+ 4p\ ^2S_{1/2} \rightarrow 3d\ ^2D_{5/2}$ transition at 729 nm in a $\text{Ca}^+ - \text{N}_2^+$ two-ion crystal

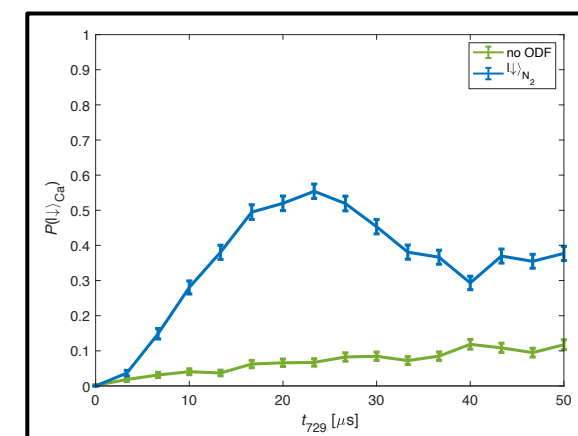
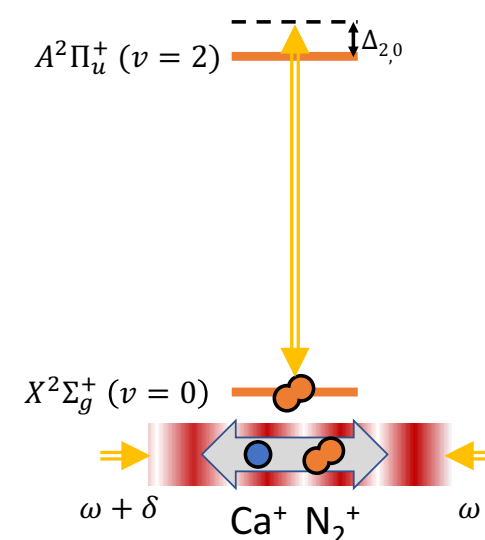
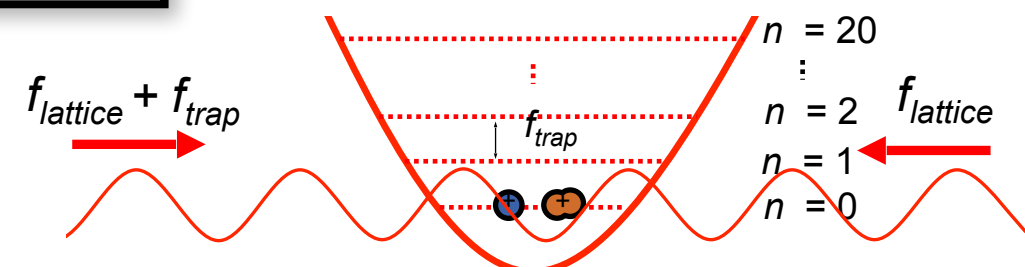
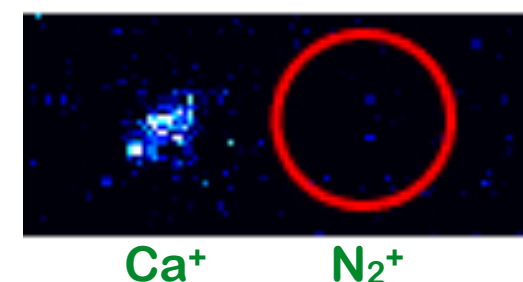


Ca⁺ spectroscopy

Quantum-non-demolition state detection of single molecular ions by coherent motional excitation of a two-ion crystal

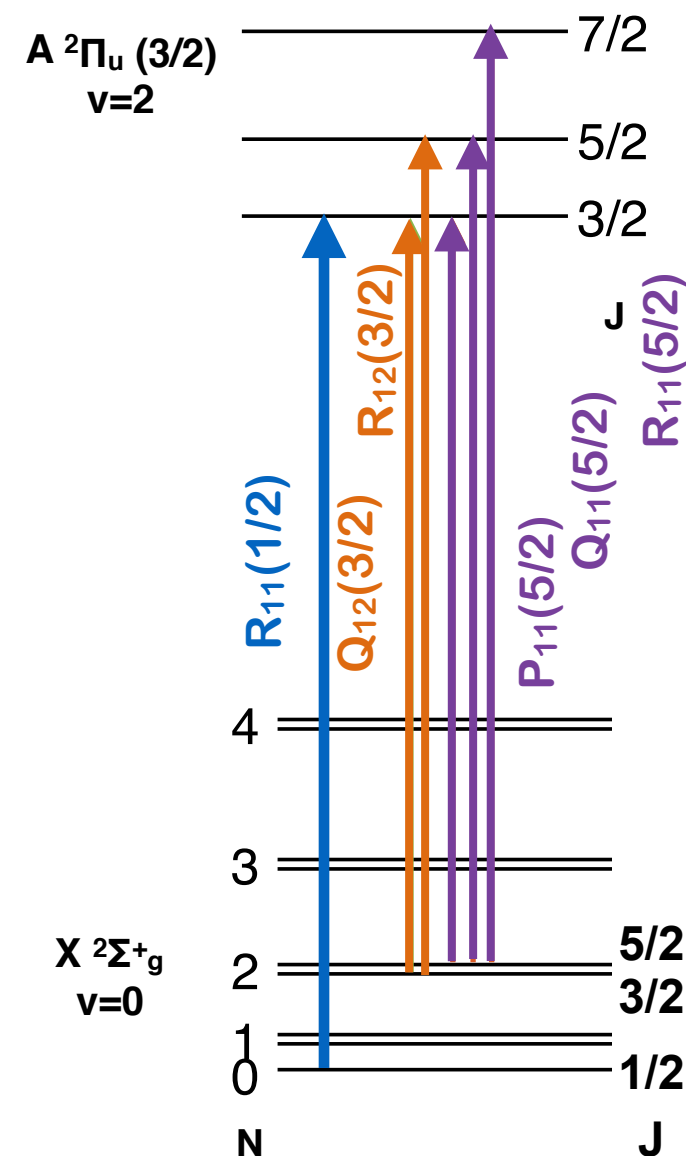
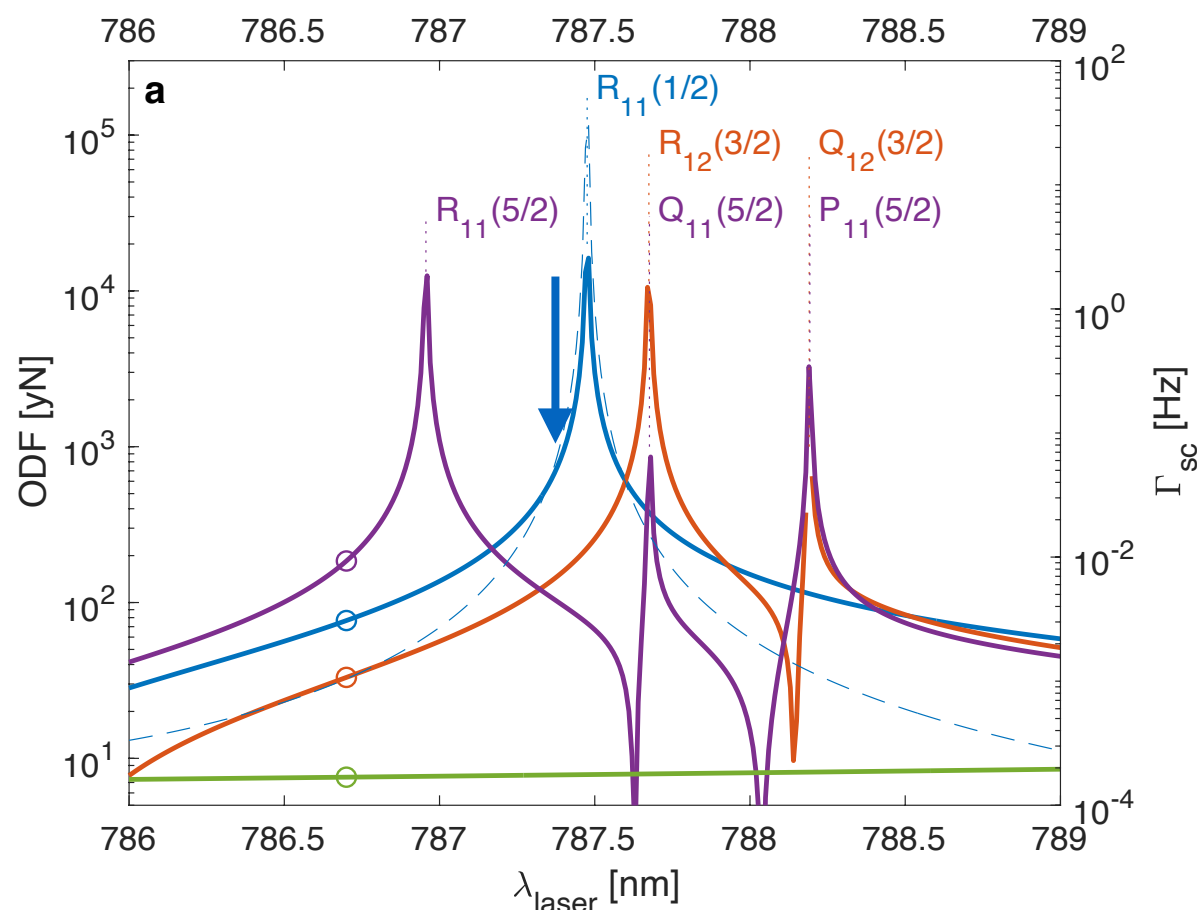
Non-destructive state-detection and spectroscopy of a single molecule

- Step 1: Preparation of a Ca^+ - N_2^+ two-ion string
- Step 2: Sympathetic cooling of the molecule to the QM ground state of the trap
- Step 3: Application of an 1D optical lattice near-resonant with a spectroscopic transition in the molecule to generate an optical dipole force (ODF)
- Step 4: Modulation of the optical lattice at the frequency of vibration of the ions in the trap to excite their motion
- Step 5: Detection of the motional excitation of the ions by sideband Rabi spectroscopy on Ca^+

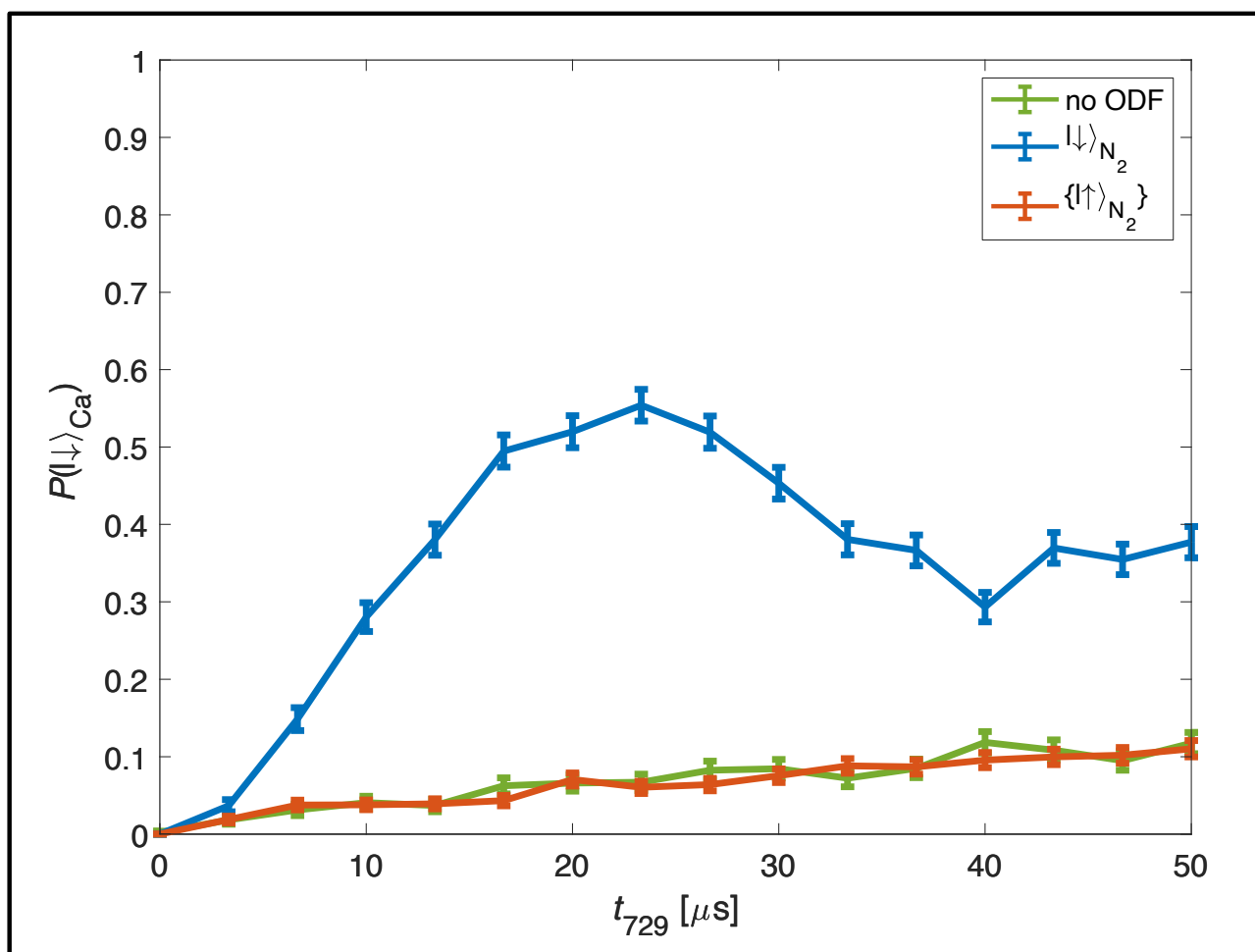


Step 3: ODF for N_2^+ in different spin-rotational states

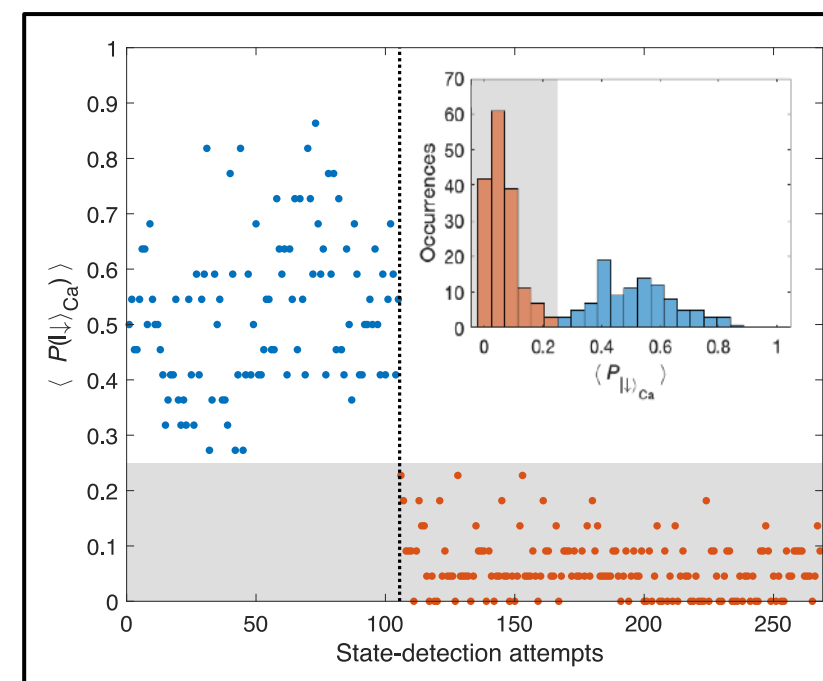
- ODF as a function of lattice-laser wavelength
- Excerpt of energy-level structure of N_2^+ with spectroscopic transitions giving rise to strong ODFs



Steps 4 and 5: Rabi flops on the $\text{Ca}^+ \text{}^2\text{S}_{1/2} \leftarrow \text{}^2\text{D}_{5/2}$ sideband transition after CME of N_2^+ in $N^+=0$

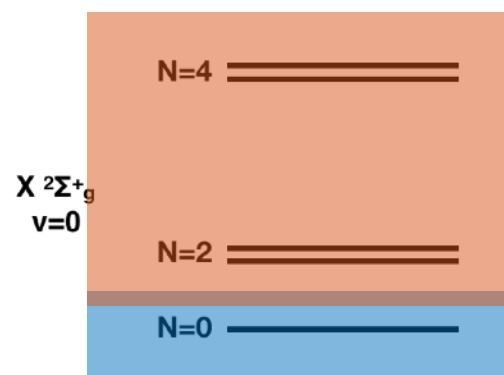


Fidelity of finding the molecule in the correct state (blue) or not (red)



99.1(9)%

99.4(6)%

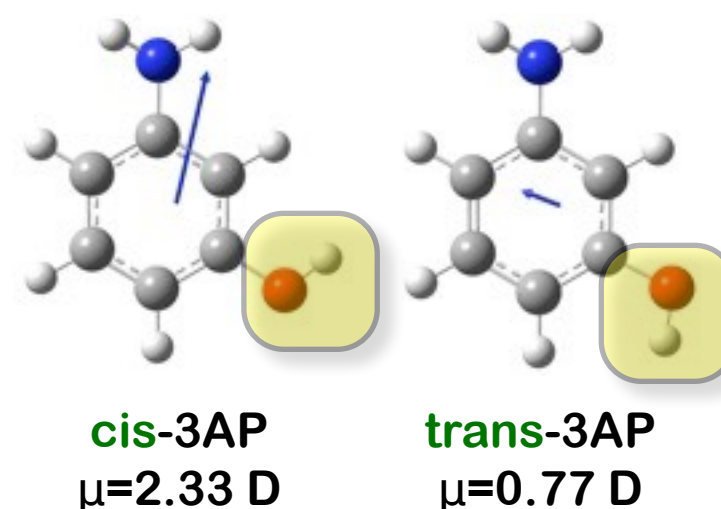


3. Applications: 2. Unravelling the details of chemical reaction mechanisms with controlled molecules

- How does chemical reactivity depend on the shape of a molecule (i.e., its conformation) ?

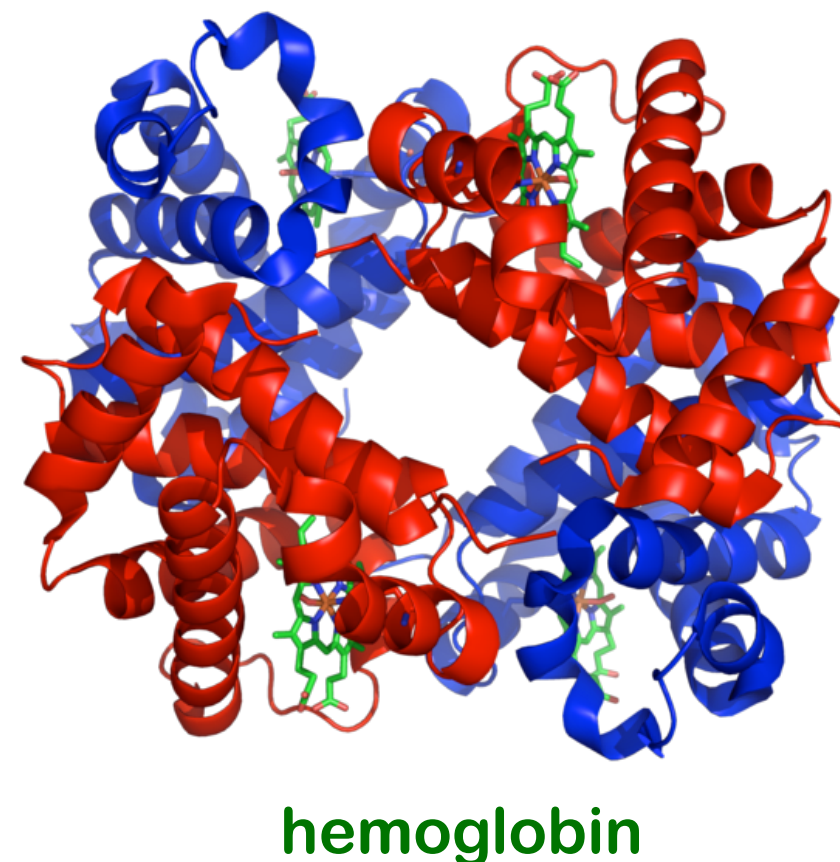
Example: 3-Aminophenol (3AP)

2 conformers: cis / trans



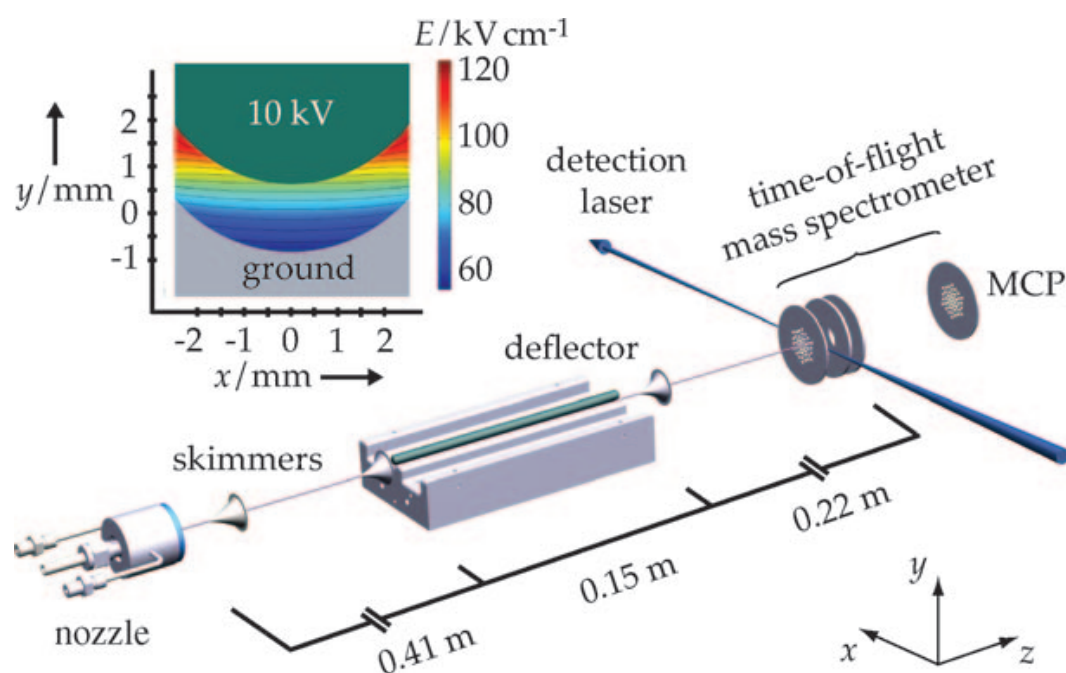
- Conformations: why bother ?

- Conformers are the dominant form of structural isomers of complex molecules, e.g., proteins such as hemoglobin.
- The chemical reactivity of complex molecules often depends on their conformation (“steric effects”)
- Conformers often easily interconvert between one another under ambient conditions: single conformers are difficult to isolate and study !

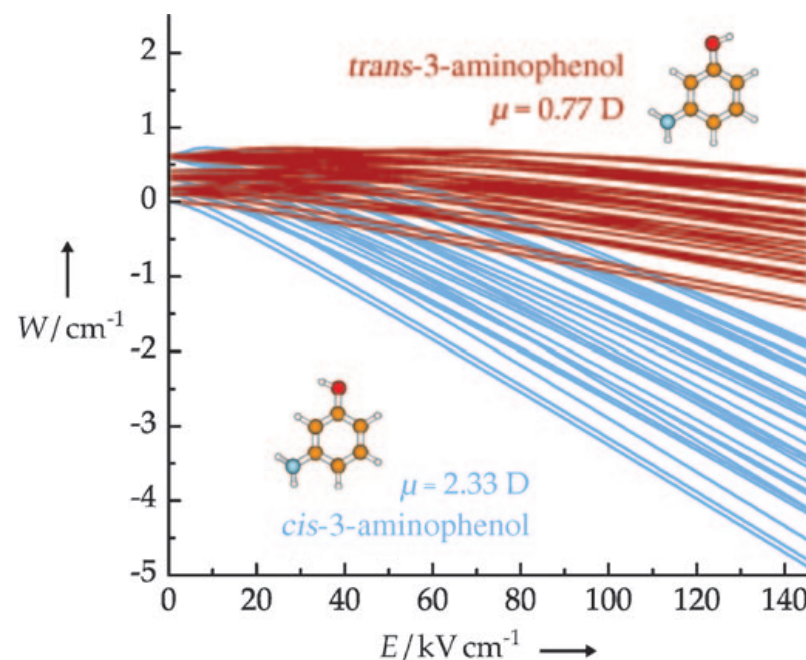


Electrostatic separation of molecular conformations in a molecular beam:

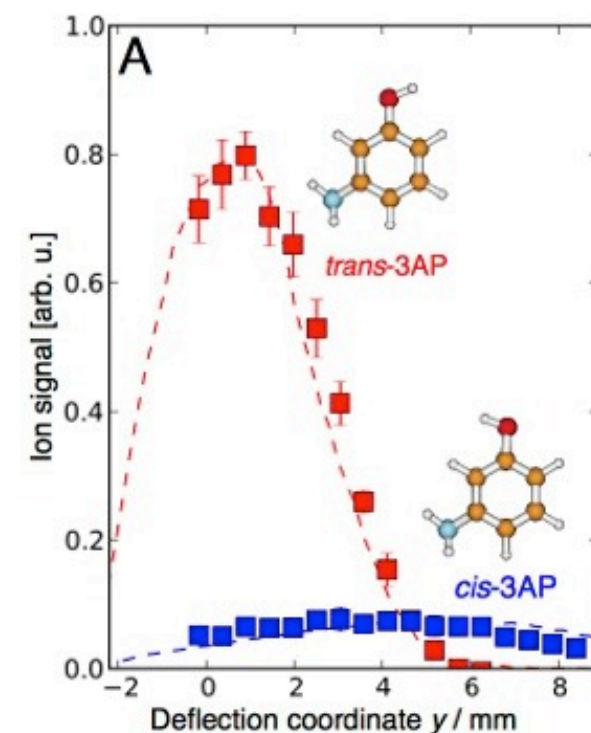
F. Filsinger, J. Küpper, G. Meijer, et al., *Angew. Chemie Int. Ed.* 48 (2009), 6900



Experimental setup



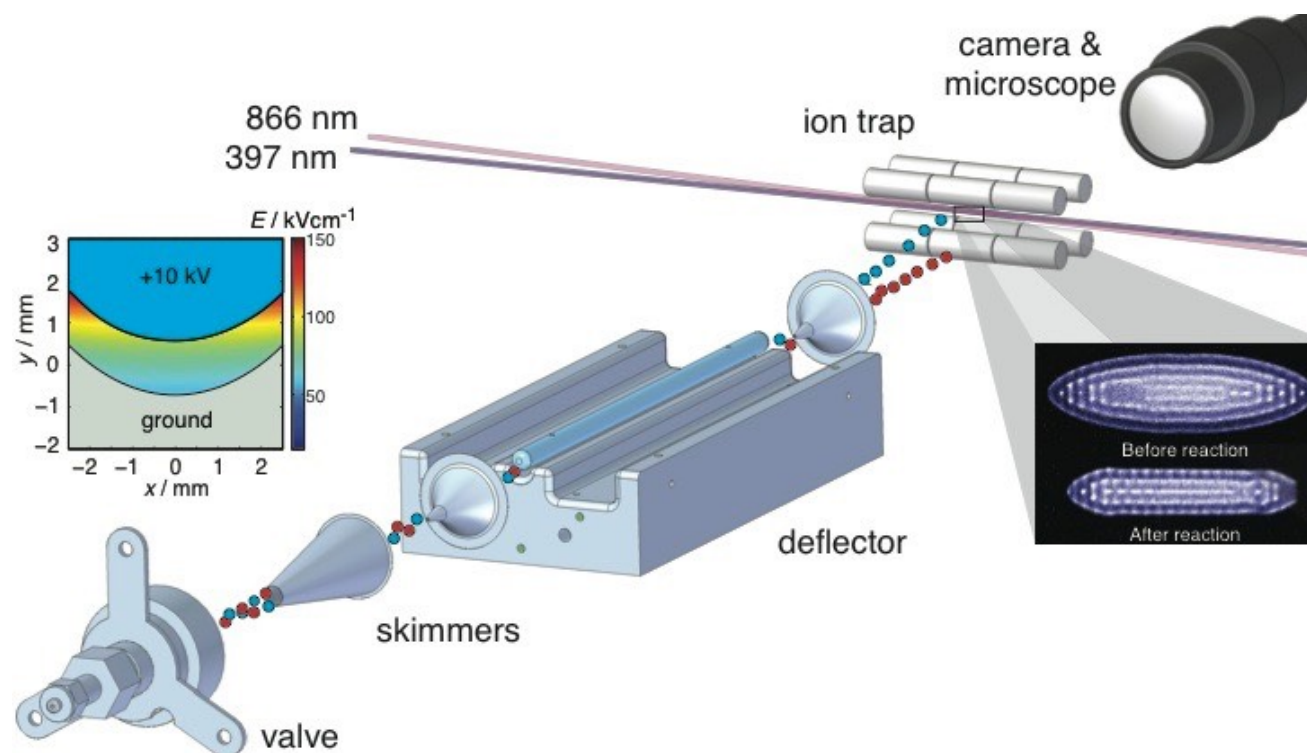
Stark energies W of the lowest rotational states of cis/trans-3-aminophenol as a function of the electric field strength E



"Deflection profiles" of cis-/trans-3-aminophenol (3AP)

Chemical reactions of selected molecular conformations:

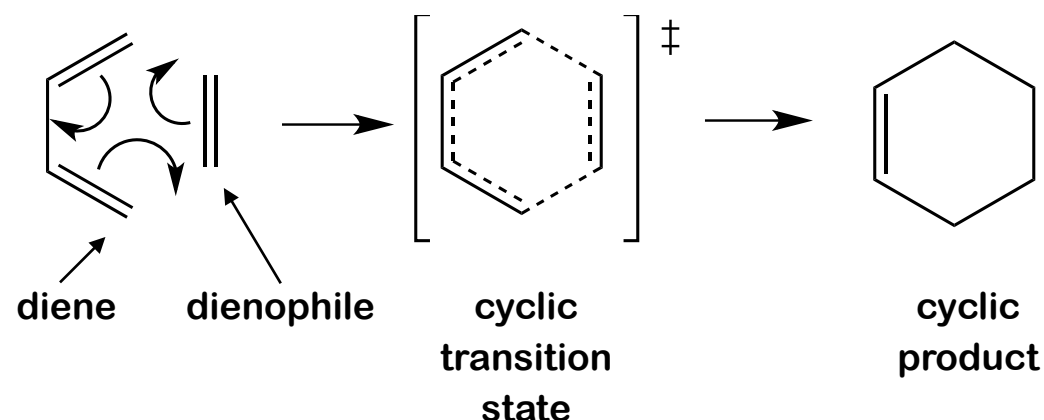
- Spatially separate specific molecular conformations from a molecular beam
- Direct the conformationally selected components of the beam at a stationary reaction target consisting of a Coulomb crystal of cold ions
- Measure conformation-specific reaction rates to probe conformation-specific chemical reactivities





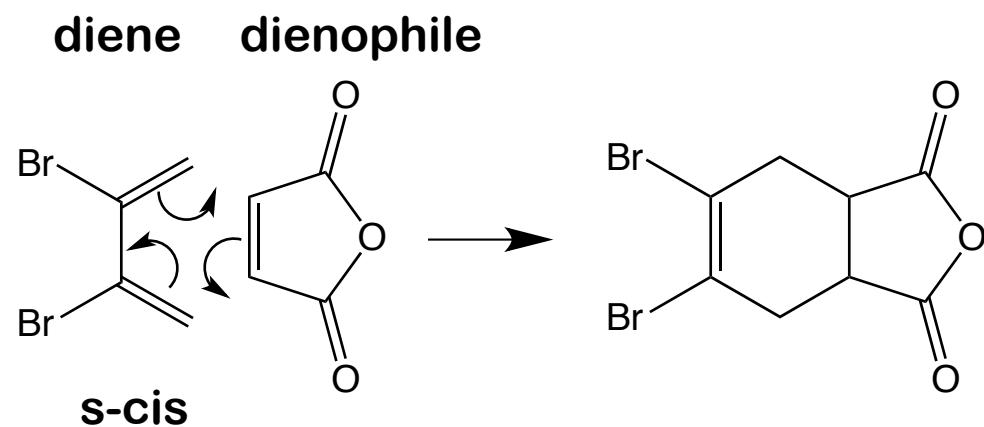
Example I: Mechanism of Diels-Alder reactions

The Diels-Alder reaction:



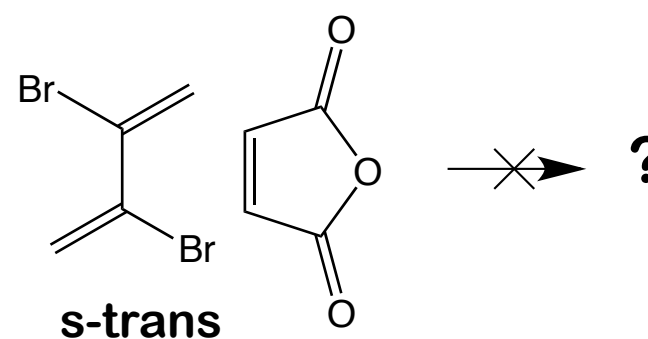
O. Diels and K. Alder, *Justus Liebigs Ann. Chem.* 460 (1928), 98

Activated Diels-Alder reactions:

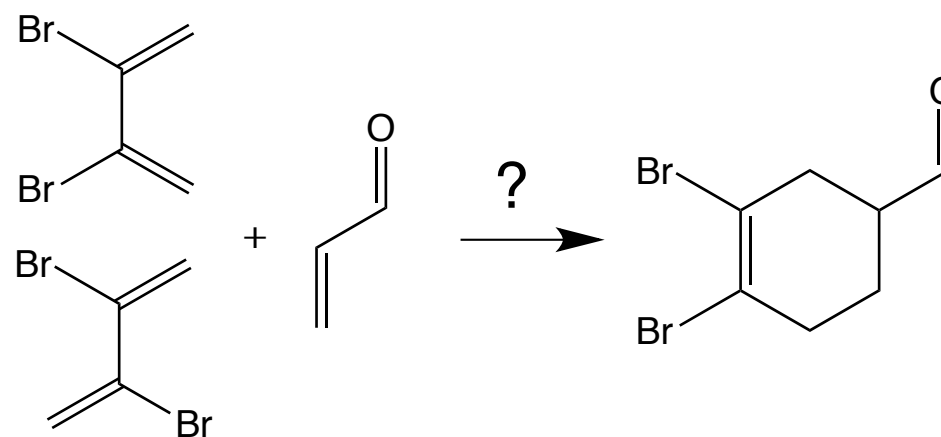


Open questions:

- Conformational selectivity

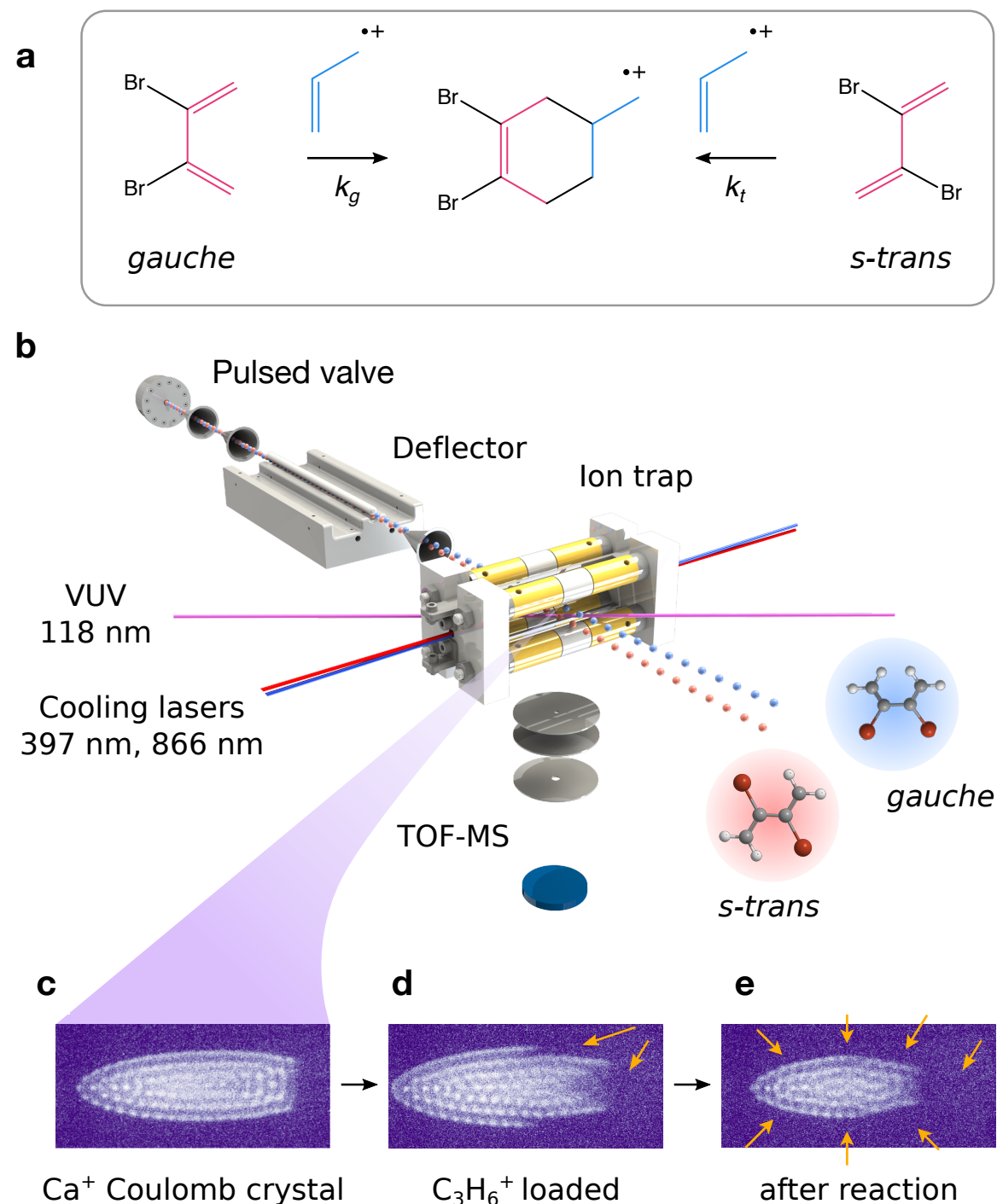


- Mechanism in asymmetric systems: concerted or stepwise, synchronicity

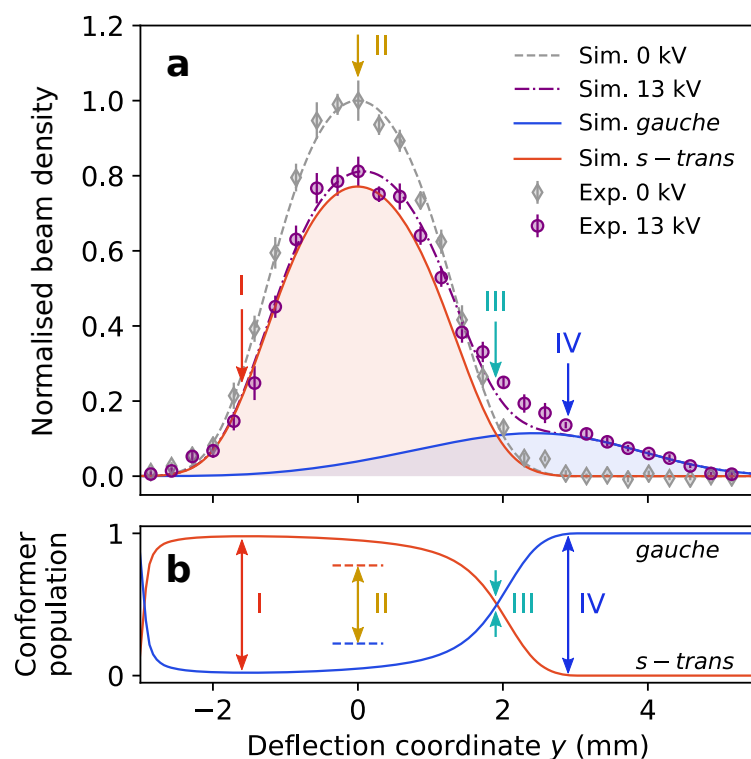


- Polar cycloadditions: effect of charge

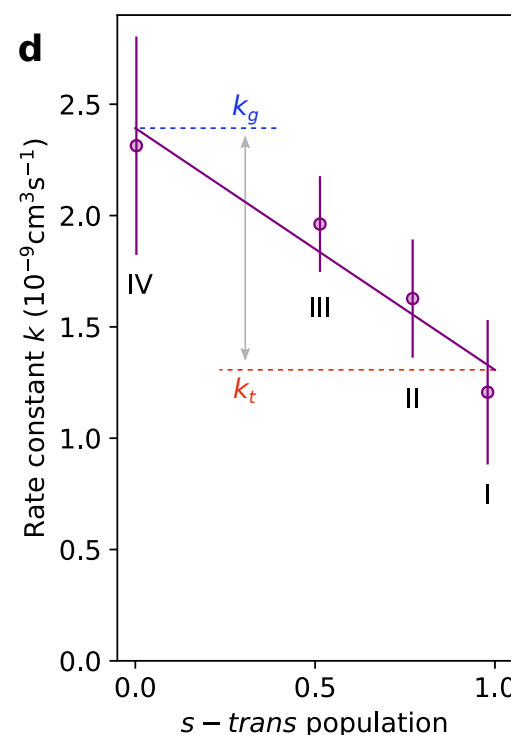
Conformer-specific polar cycloaddition of 2,3-dibromobutadiene with propene ions



Reaction rates of *s*-trans- and gauche-DBB: both conformers react



**Deflection profiles of
2,3-dibromobutadiene
(DBB)**

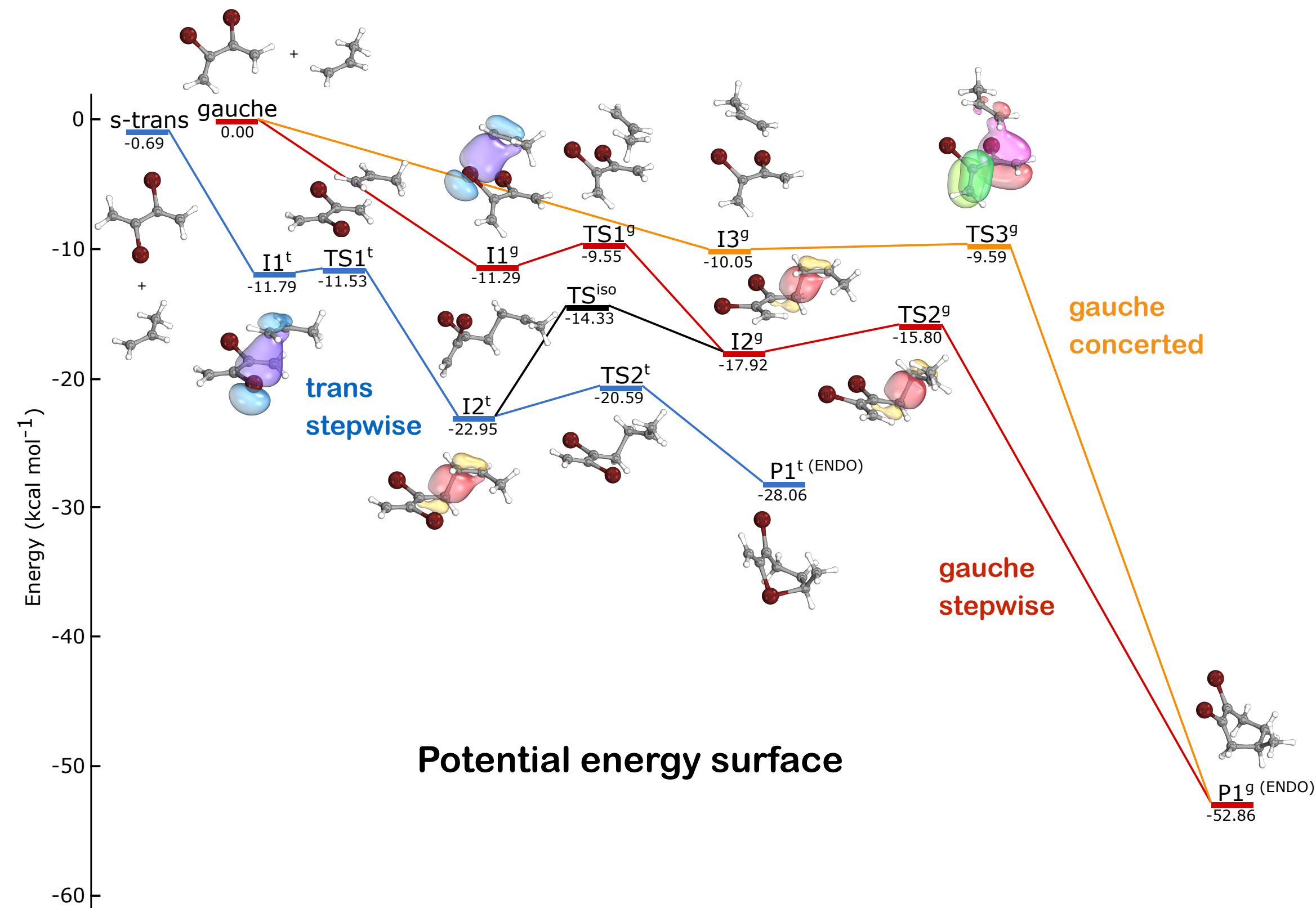


**Bimolecular rate
constants as a function
of the relative
conformer population**

- Both conformers react fast (capture limited) !
- gauche*-DBB reacts 60% faster than *trans*-DBB



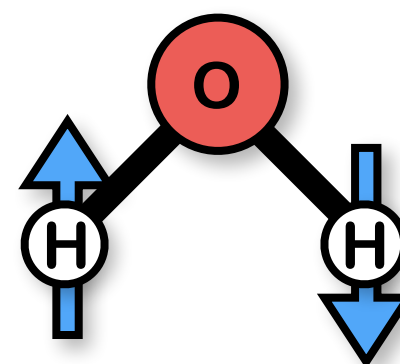
Rationalisation: simultaneous competition of concerted and stepwise reaction mechanisms involving both conformers



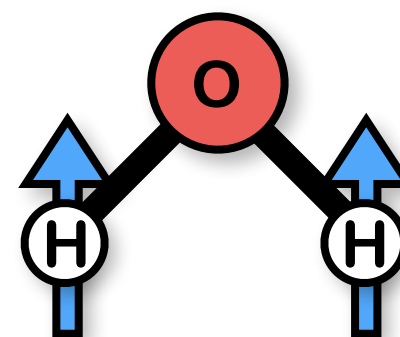
Example II: Different reactivities of ortho- and para-water

A. Kilaj, H. Gao, D. Rösch, U. Rivero, J. Küpper and SW, Nat. Commun. 9 (2018), 2096

- Like H_2 (see Sec. 2.1.3), water H_2O consists of two nuclear spin isomers ortho (o, $I=1$) and para (p, $I=0$)
- The interconversion between the two isomers is in principle forbidden in isolated molecules, by dipole radiation and by dipole collisions
- Interconversion rates between the two isomers are still disputed in the literature
- Because of the generalised Pauli principle, they are associated with different rotational wavefunctions (like in H_2 , Sec. 2.1.3)
- Is there a difference in their chemical reactivity ?



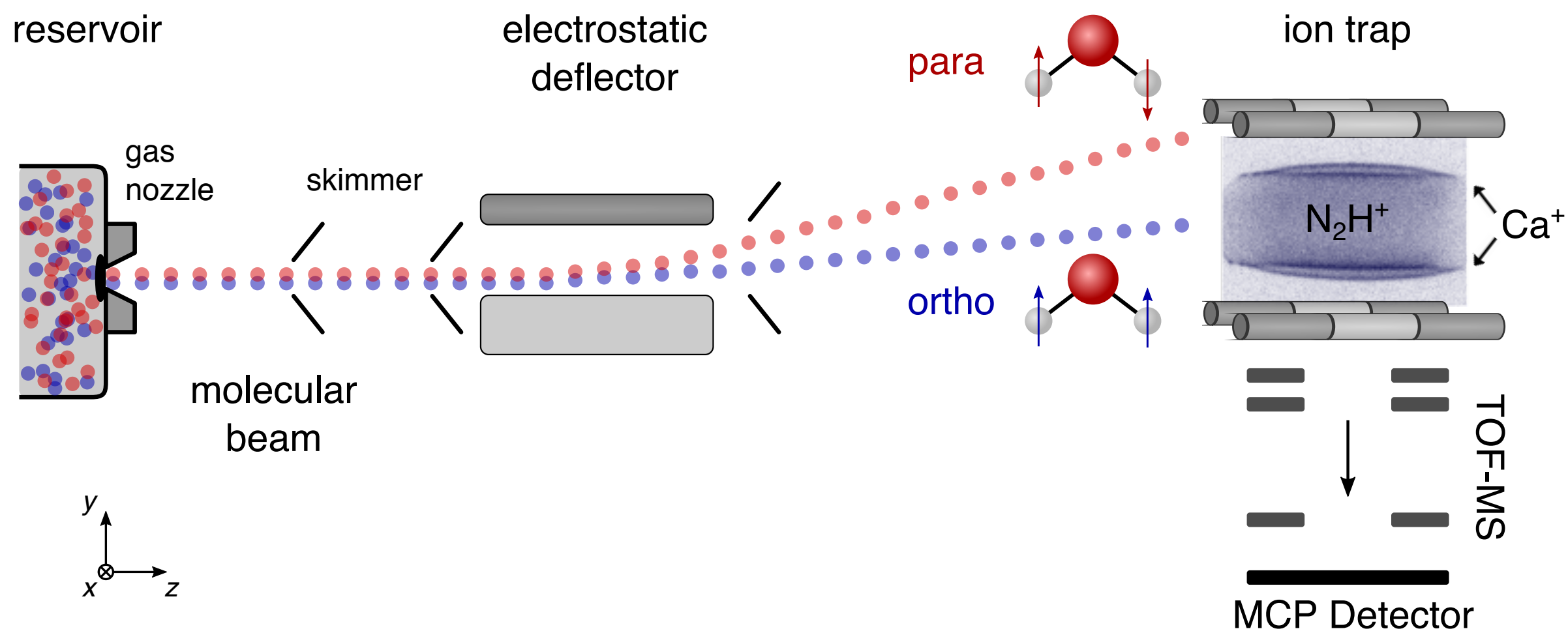
para ($I=0$)
 $K_a K_c = ee$ or oo
 ground state:
 $J_{K_a K_c} = 0_{00}$



ortho ($I=1$)
 $K_a K_c = eo$ or oe
 ground state:
 $J_{K_a K_c} = 1_{01}$



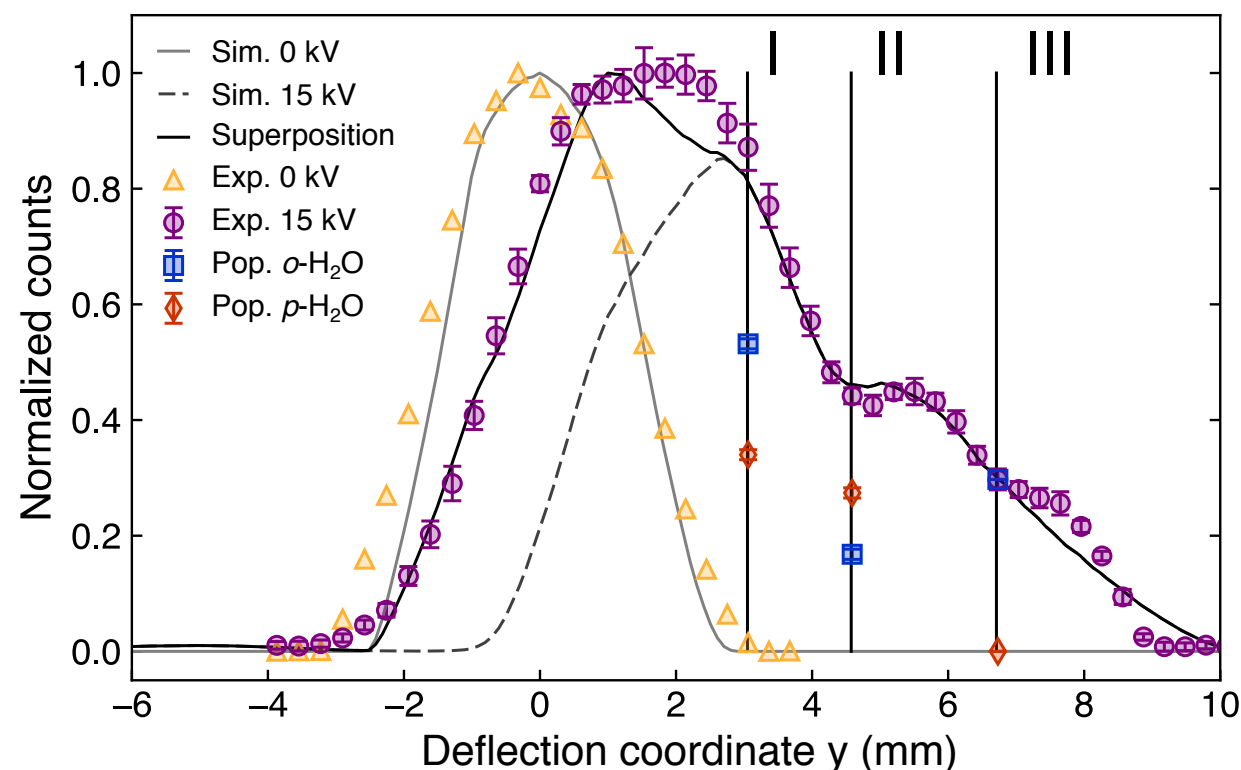
Target reaction: $\text{H}_2\text{O} + \text{N}_2\text{H}^+ \rightarrow \text{H}_3\text{O}^+ + \text{N}_2$



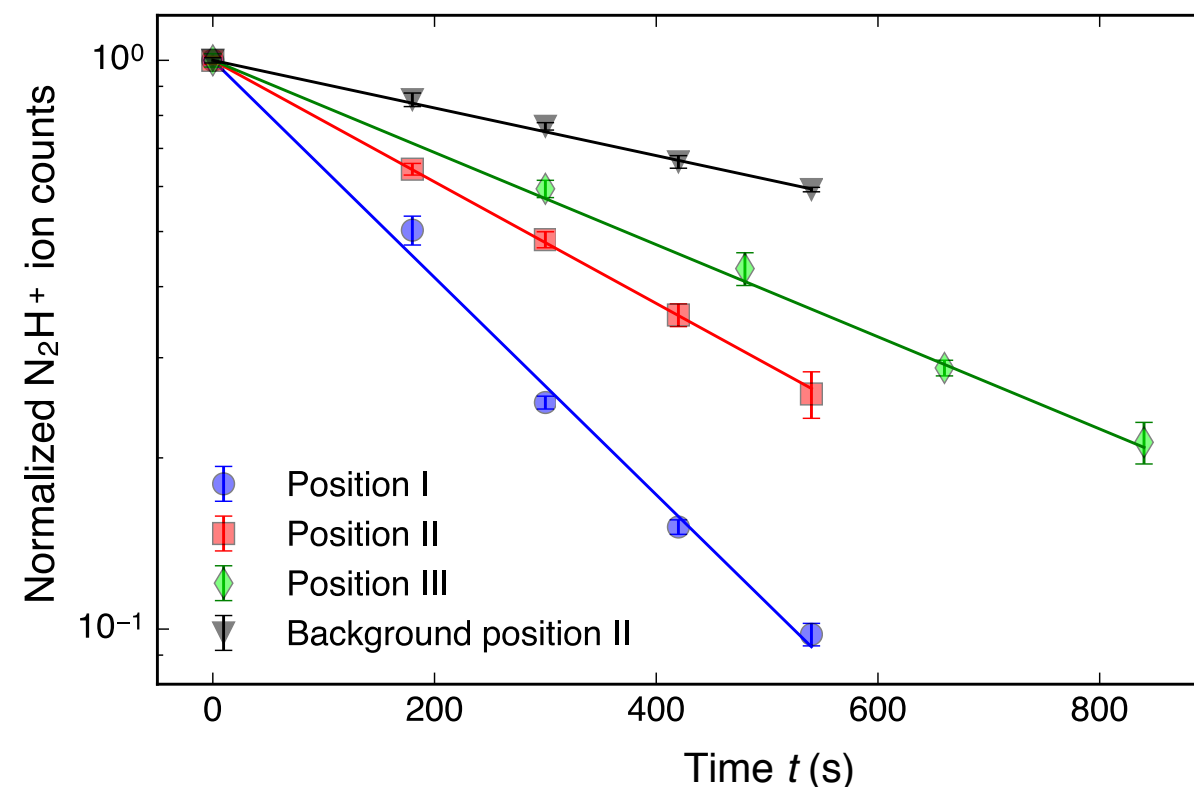


Reaction rate measurements

Deflection profile



Pseudo-first-order reaction rates at positions I, II and III



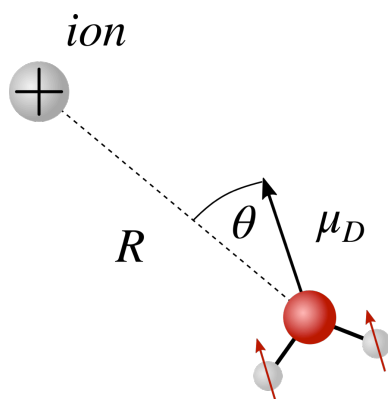
Second-order rate constants:

- $k(\text{para}) = 6.0(10) \times 10^{-9} \text{ cm}^3 \text{ s}^{-1}$
- $k(\text{ortho}) = 4.8(9) \times 10^{-9} \text{ cm}^3 \text{ s}^{-1}$
- relative difference: 23(9) %
(as inferred from pseudo-first order rate const.)

Rationalisation of results: adiabatic capture theory

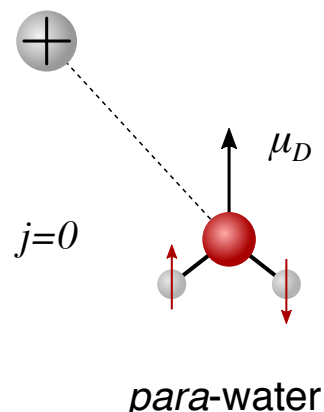
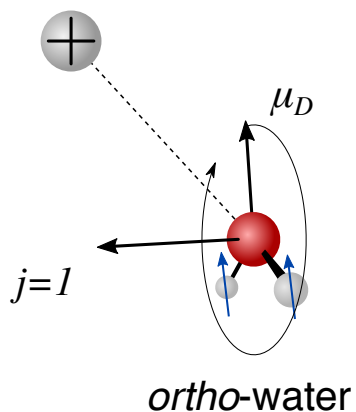
D.C. Clary, J. Chem. Soc. Faraday Trans. II 83 (1987), 139; T. Stoecklin et al., J. Chem. Soc. Far. Trans. 88 (1992), 901

Long-range interaction potential:

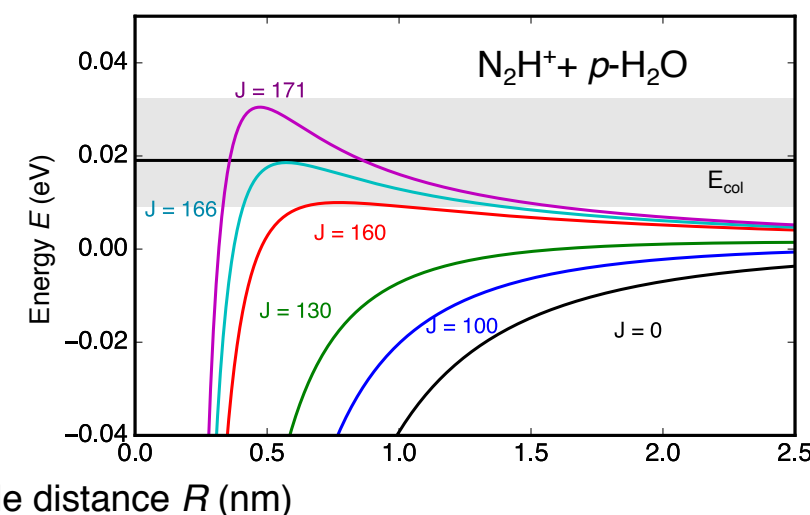
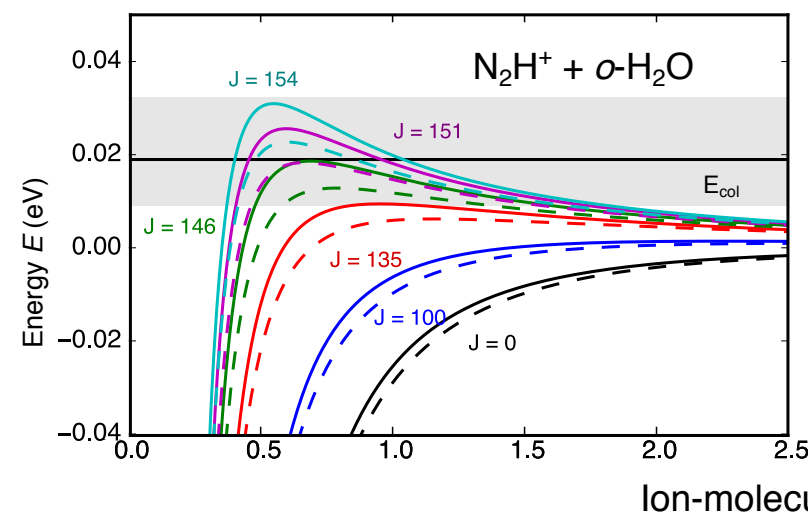


$$V(R, \beta) = -\frac{\alpha q^2}{2R^4} - \frac{q\mu_D \cos \beta}{R^2}$$

charge-induced dipole
charge-permanent dipole



Centrifugally corrected rotationally adiabatic potentials for H₂O (J_{K_aK_c}) + N₂H⁺

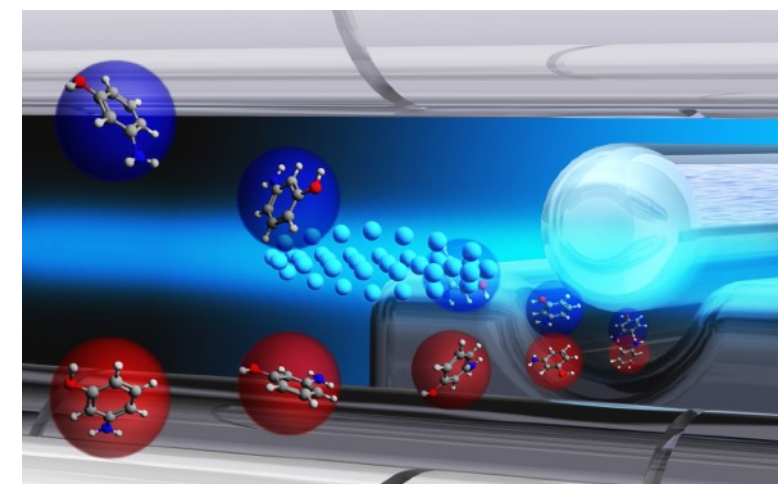
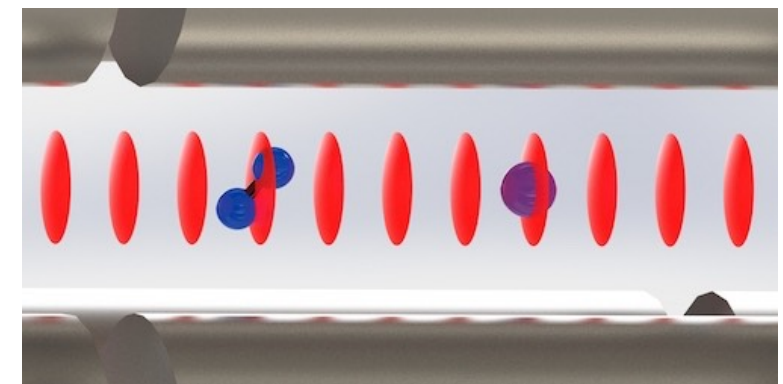
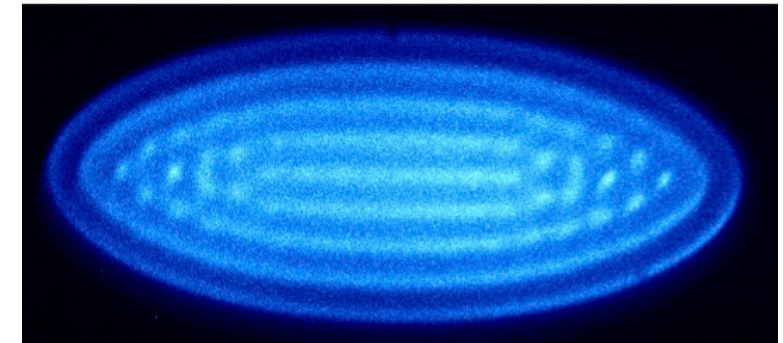


Relative difference of rate constant according to adiabatic capture theory: 24(5) % (expt.: 23(9) %)

Conclusion: The difference is due to different rotational averaging of ion-dipole long-range interactions for the two nuclear-spin isomers.

Summary

1. Cold molecular ions represent a versatile and powerful platform for performing highly controlled experiments on the single-particle level
2. Applications range from molecular quantum technologies over precision spectroscopy to accurate studies of chemical reaction mechanisms



Acknowledgements

